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# DESIGN AND DEVELOPMENT OF RYERSON FEMTOSATELLITE

by

Bryan Stuurman B.Eng Ryerson University 2007

A thesis presented to Ryerson University In partial fulfillment of the requirement For the degree of Master of Applied Science in the program of Electrical and Computer Engineering

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## **DEDICATION**

This thesis is dedicated to the hardworking members of laboratory EPH132. Without your encouragement, assistance and distraction none of this would have been possible.

#### ABSTRACT

# Design and Development of Ryerson FemtoSatellite

Master of Applied Science 2009, Bryan Stuurman Electrical and Computer Engineering, Ryerson University

This thesis describes the design and development of Ryerson University's femtosatellite. The motivation for this project is to achieve a new level of miniaturization of a satellite system to reduce costs and development time. A design is presented which demonstrates attitude control, earth contact capability and basic satellite functionality. This design weighs less than 100 grams including a 25 gram payload capacity. Earth observation and inspector satellite payloads are the proposed missions for this spacecraft. A prototype was constructed and its various subsystems functioned to their design capacities.

#### ACKNOWLEDGMENTS

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## NOMENCLATURE

$A,\overline{A}$	Area $(m^2)$
$A_{bi}$	DCM describing the rotation from the inertial frame to the body frame
В	Magnetic field (tesla)
$C_d$	Drag coefficient (dimensionless)
$\delta^i_j$	Kronecker delta function
Eye <sup>3</sup>	3x3 identity matrix
ε	Quaternion imaginary components
f	Frequency (Hz)
Н	Kalman filter observation matrix
I,i	Current (Amperes)
I <sub>sat</sub>	Satellite inertia tensor $(kg \cdot m^2)$
Κ	Kalman filter gain matrix (9x1)
L	Inductance (Henries)
$L_s$	Space loss in communications link $(dB)$
$ar{M}$	Magnetic dipole moment $(amp \cdot turn \cdot m^2)$
η	Quaternion scalar component
$N_d$	Demagnetization factor (dimensionless)
Ν	Number of turns (dimensionless)
ρ	Atmospheric density $(kg / m^3)$
$ \rho_{nnnkm} $	Earth angular radius (rad)
q	Unit quaternion describing rotation (dimensionless column vector $4x1$ )
Q	Kalman filter process noise (3x3)
R	Kalman filter measurement noise (3x3)
S	Communications path length (m)
Р	Kalman filter error covariance matrix (9x9)

$R_E, R_{Earth}$	Earth Radius (6378000 meters)
t	Time (seconds)
τ	Torque (Nm)
и	Control effort (Nm)
$\mu_r$	Magnetic permeability relative to free space (dimensionless)
$V(r,\theta,\phi,t)$	Scalar potential function of geocentric radius, coelevation, east longitude and time
V	Kalman filter innovation vector
V	Voltage
$V, \hat{V}, ar{V}$	Orbital velocity $(m/s)$
$\omega, ec \omega$	Angular rate (rad/s)
Χ	State vector
χ	Linearized system state vector
Ω	Orbital angular velocity

## ACRONYMS

ADACS	Attitude Determination And Control System
AWG	American Wire Gauge
CMOS	Complementary Metal Oxide Semiconductor
COTS	Commercial Off The Shelf
dB	Decibels
dBi	Decibels with respect to an isotropic radiator
dBm	Decibel milliwatts
DC	Direct current
DCM	Direction cosine matrix
DOF	Degrees of Freedom
DMA	Direct Memory Access
DUT	Device under test
EKF	Extended Kalman Filter
EMI	Electromagnetic interference
FIFO	First In Fast Out
GPS	Global Positioning System
IC	Integrated circuit
IGRF	International Geomagnetic Reference Field
LEO	Low Earth Orbit
MEMS	Micro Electro-Mechanical Systems
MPPT	Maximum Power Point Tracker/Tracking
PCB	Printed Circuit Board
PWM	Pulse Width Modulation
RMS	Root mean square
SOC	System On a Chip
0xNN	Denotes a number given in hexadecimal representation

# Chapter 1 Introduction

The design and launch of a large orbital satellite is a costly endeavor. Since the first satellite launch in 1957, satellite systems continue to grow in mass and size to meet mission objectives, despite increasing levels of miniaturization in the electrical systems that the satellites employ. Small satellites are now becoming the satellite of choice for research institutions to demonstrate technology and accomplish simple scientific missions (Alger, 2008). It is hoped that these small satellites can cause a shift in the design philosophy of conventional satellites, and encourage the space industry to shift to a less expensive, faster to deploy strategy in leveraging orbital technologies.

Recently, concern over orbital debris has grown due to anti-satellite activities by the American and Chinese governments, and due to the collision of a derelict soviet radar satellite and an Iridium constellation satellite (Iannotta and Malik, 2009). Mission designers need to consider the end of life disposal of their craft. The usage of a small satellite constructed of demiseable materials can lead to less orbital debris. A small satellite is easier to de-orbit and has a low probability of on orbit breakup.

Forthwith a design is proposed to reduce the satellite system launch mass to less than 100g, and to reduce the component count to the bare minimum required for a functional satellite. The design will demonstrate the capacity for a number of relevant missions, some of which are not possible with larger satellite systems.

#### 1.1 Motivation

Classically, the space industry is the most conservative of all the aerospace sectors, preferring to leverage only the qualified of flight hardware. Significant prejudice is given to components with flight heritage, even if the technology exists to improve upon these components. Managing risk is an important part of a mission designer's job and building a newer, faster, smaller subsystem carries huge risk over employing an older, slower, larger subsystem that has proven its capacity for reliable operation. This attitude has lead to the ballooning of mass and volume requirements, the culmination being the largest telecommunications satellite ever launched: TerreStar 1. TerreStar 1 had a system bus mass of 6910 kg, and required a 145 kg payload adapter for a total launch payload of 7055 kg. This satellite was carried into earth orbit by an Ariane 5 launcher. The total cost of the satellite, launch and insurance is estimated to be over 500 million dollars (Marot, 2009).

Large spacecraft suffer a number of disadvantages, the biggest being cost. Between the cost of individual subsystems to the cost of launch and maintenance, these satellites consume money every step of the way. This large consumption of money drives the culture of risk management, where no component shall be permitted to fail and compromise the mission. This reliability comes at increased cost, and decreased flexibility in fulfilling the mission requirements. This is a vicious cycle, where cost rises and launch opportunities decrease.

Small satellites benefit from just the opposite design philosophy. Risk is embraced in expectation of higher returns. Instead of managing risk, commercial-off-the-shelf (COTS) components are leveraged to manage cost. Low cost-high risk missions are justifiable as the success of the mission results in substantial return on investment, where the cost of failure is inherently minimized due to the inexpensive nature of the mission.

Small satellites also offer the opportunity for innovative new mission configurations, where payload capabilities are replicated or distributed across multiple satellites flying in formation. Formation flight is inherently cheaper with lower mass satellites, possibly even free if

environmental forces can be utilized to achieve the formation. Larger satellites are generally not considered candidates for close formation flying.

Compared to large satellites which can take years to design and launch, small satellites often proceed through the design cycle rapidly, sometimes taking advantage of immediate COTS component availability to perform breadboard subsystem tests in mere weeks. This leads to the hardware being developed in parallel with the mission requirements, and the hardware design being flexible to requirement changes. Large satellite equipment is fraught with lead times, bulk orders for special items, regulatory hurdles to procurement and large price tags. Parallel development of a satellite comes with the risk that the components chosen will not fulfill the end requirements. Should this occur with a large satellite, the result would be devastating in terms of cost and development time, whereas with a small satellite the loss is limited to small dollar sums and minimal time expense.

The motivation of this project is to push satellite design to a new level of miniaturization. The femto class of satellites has never been achieved with the proposed capabilities. Small disposable satellites can achieve cost and time-to-launch reductions which larger satellites cannot. Furthermore this design will offer "trickle down technology" – the degree of miniaturization employed in this study can be applied to larger satellites, likely of pico- and nano- class, to increase payload capacity and as such offer a higher return on investment on small satellites.

#### **1.2 Literature Review**

This literature review will cover relevant material to the design presented in this study. Femtosatellite proposals similar to electronic microchips are first discussed, then femtosatellites constructed from a printed circuit boards are covered. Printed circuit board satellites are considered state of the art as they stand the greatest chance of mission success. Finally, picosatellites and specifically cubesats are discussed to grant insight into current amateur and small satellite design paradigms. A femtosatellite is a satellite with a mass of 100 grams or less. To date and to the authors knowledge, no femtosatellites have been flown with the technical exception of the US government radio experiment *Project west ford*, which placed 480 million copper dipoles into a 3200 km orbit (Larson and Wertz, 1999). Being passive orbiting objects, we can consider the project (called "Needles" in-house) an inadequate representation of what femtosatellite capabilities should be. Furthermore the project was a public relations failure due to the perceived orbital debris hazards the project created to spacecraft and astronauts at the time.

Femtosatellite design has been investigated formally since the late 1990's, with significant early efforts exerted by The Aerospace Corporation. Femtosatellites grow from the space industries need to reduce flight mass to reduce launch costs, which encourages suppliers to develop innovative new ways to solve typical mission challenges. Since actuators on a spacecraft necessarily scale with the size and inertia of the craft, which is in turn dictated by payload, initial efforts were put towards application of micro electro-mechanical systems (MEMS) and micro fabrication techniques to miniaturize sensors. The philosophy is that greater benefits to the aerospace community can be achieved through the miniaturization of sensors, which would scale independently of vehicle mass. (Smit, 1997) The reduction in sensor size available with MEMS and the corresponding increase in the computational abilities of commercial microelectronics, with decreasing electrical power and physical space requirements, now lead the push for a fully miniaturized spacecraft. At the extreme end of this push is the community looking to fabricate an entire satellite on a silicon wafer, in the same manner as typical system-on-a-chips are currently fabricated. Such a satellite would be incredibly low cost in volume, and exceptionally light, and as such the mission cost would be small.

#### 1.2.1 Satellite on a chip

A satellite or significant fraction of a satellite, fabricated onto a silicon wafer shows some advantages over a conventional design approach. Firstly, a high level of integration can be achieved through miniaturization. Secondly, power requirements for MEMS sensors and actuators are significantly lower than their larger counterparts. Furthermore, while a fabrication process for a system on a chip can be expensive in money and time to design and implement, economies of scale being to take effect during production, where thousands of satellites can be fabricated with low lead time and little additional cost.

Silicon as a structural material is rather effective, having a higher yield strength than aluminum, titanium and stainless steel, while being less dense than all three. The thermal conductivity of silicon is less than that of aluminum (150 W/mk versus 240 W/mk), however silicon's coefficient of thermal expansion is similar, and its melting point is more than double. Silicon is much more brittle than aluminum or titanium, but due to the significant reduction in launch mass and size, it is expected that the resultant structure would survive the launch environment (Janson, 1999).



Figure 1.2-1 Yield strength vs. mass density for various materials (Janson, 1999)

Current satellite-on-a-chip efforts are hindered by several technology limitations: Solar cells, a primary energy source for space systems, cannot be fabricated with current CMOS processes (used for System On a Chip fabrication). Additional complications arise when requiring energy storage, due to the substantial surface area a chip level capacitor would require (Barnhart, 2006).

Further issues arise from on chip antennas, which have limited range, to a maximum of 5 meters, requiring close proximity of a much more powerful radio transponder and the

associated formation keeping requirements. Upper atmospheric effects such as atomic oxygen are especially detrimental to the survivability of the craft, as are the thermal extremes of an effectively passive thermal node in earth orbit. (Barnhart, 2006)

#### 1.2.2 State-of-the-art

Major David Barnhart and the team of researchers at Surrey Space Center have put forth two concepts: a satellite on a PCB, and a satellite on a chip. Both of these are presented in their paper "A low cost Femtosatellite to enable distributed space missions". The less extreme concept of a femtosatellite is the assembly of several highly integrated SOCs in addition to their supporting components to fulfill the requirements of a complete spacecraft. Typically these designs seek to minimize the additional mass cost associated with multiple module integration and require many parts to perform more than one task. As a result, the proposal of the Printed Circuit Board satellite (PCBSat) is being actively developed to fill the intermediate gap between picosatellites and satellites on a chip.

The attractive features of a PCBSat are its significantly larger area, ability to integrate several subsystems from different processes, and ease of manufacture. COTS components are leveraged wherever possible to reduce construction costs and take advantage of cumulative industry experience.

PCBSats are constructed of circuit board or circuit board clamshell. Circuit boards are typically constructed from FR4 glass epoxy and can contain several layers of copper traces inside and on its surface. FR4 is a common material in electrical engineering and has several decades of proven performance behind it. Densities are typically in the range of  $1400kg / m^3$  and a tensile yield strength of around 240MPa. This is a yield comparable to aluminum with only 52% of the mass penalty, which is attractive, and good justification for using FR4 as a structure. Being less ductile than aluminum the design must prevent the FR4 from being stressed into distortion, otherwise de-lamination and failure will occur rapidly.

Introduction

PCBSats typically contain few provisions for attitude control. McVittie and Kumar propose a tethered formation of two identical units, each with a single magnetic torque coil (McVittie and Kumar, 2007). The expectation is that the tethered structure will eventually tighten in orbit and become gravity gradient stable, while the single axis magnetic torque rod can be used to dampen rotation about the nadir. Similarly Barnhart et al. propose a similar design with a single magnetic torque coil, without the addition of a gravity gradient formation. (Barnhart, 2009) One notable exception to this is the 100g inspector satellite proposed by Huang et. Al. which uses an array of micro thrusters and a 5cc fuel tank aboard a 50x50x50 mm satellite fabricated using photostructurable glass/ceramic materials. These thrusters can be used for attitude and orbit control, and the whole motion module weighs less than 45 grams. (Huang, 2002)

There are particular challenges which need to be addressed with the two PCBsat proposals in order to make the designs space-worthy. Below is a discussion of their shortcomings.

#### Barnhart/Surrey PCBSAT:

It should be noted that Barnhart acknowledges that the existing prototype PCBsat was not designed with the space environment in mind. Instead their prototype is intended as a payload module for EyaSat *the classroom satellite*<sup>TM</sup>. EyaSat is a satellite system trainer for aerospace engineering students, and is not flight-able. With this in consideration, the issues limiting the space-worthiness of the Barnhart PCBsat will be addressed.

The communication subsystem does not have enough broadcast power to reach earth from LEO. Instead the satellite must be in close proximity to a larger satellite with ground contact capabilities to be useful. Formation flying with this larger satellite is not addressed, and could limit mission lifetime as differential drag separates the PCBSAT from its mother ship. While this does not mean the mission is unfeasible, it does limit the capabilities of the satellite and its mission.

Attitude control is not formally addressed with the especially under-actuated single magnetic actuator case. The attitude paper referenced is specifically for drag stabilized satellites with 3

7

axis magnetic dipole control. The method of attitude control presented by (Psiaki, 2004) uses three deployed vanes to create a badminton style shuttle-cock to create aerodynamic stiffness about the pitch and yaw axis. Stability is then achieved with active magnetic torque rods on all three axes.

The proposed design is actually double the weight of a formal femtosatellite after integration into the flight structure. While the PCB of the PCBsat is only 70 grams, the proposed budget for the enclosed Femto is 200 grams.

The maximum power point tracking (MPPT) circuit proposed from the Maxim application note (Maxim, 2000) is designed to track only a single voltage point in the solar arrays VI curve. This point is chosen in the application note to be the "typical" maximum power point for an earth based cell, which benefits from a moderate thermal environment and suffers from slightly lower insolation. In the orbital environment the temperature of the array can rise to a maximum (equilibrium) of 122 degrees Celsius (Wertz 2009). The internal resistance of the solar cell increases with temperature, and hence the MPP voltage drops. The converter proposed will not track the MPP in this case.

Finally the antenna appendages significantly increase satellite cross section without being treated as deployable appendages. Without some form of active antenna deployment or redesign of the particular radio systems using these antennas the satellite will not fit in the P-POD launcher as proposed.

McVittie and Kumar /Ryerson Space Systems Dynamics and Control "Ryefem" PCBsat:

McVittie and Kumar propose a similar electrical design to Barnhart/Surrey with some flightability issues. While most of the issues presented are not complete failures of the design, they do stand between the design and a complete spacecraft. They are reviewed below.

The radio module proposed comprises almost 20% of the mass budget of the Femtosatellite. This unit offers a tradeoff in the design: ground contact is probably achievable using this module as shipped, however the mass penalty is large.

8

Ultra-capacitor energy storage is significantly less mass efficient than lithium polymer batteries, and as a result the ultra-capacitor design can only operate for very brief bursts. Sustained operation during eclipse does not appear feasible due to the limited energy storage capabilities of the ultra-capacitor.

The dual satellite tethered configuration actually makes this Femto 200g, since the other Femto is required for attitude stability. Further each Femto is a clone of the other, yet only one appears to fulfill the mission set out to it. This either results in the waste of half the satellite system or the mission/satellite must be modified to be functional even when pointing in the negative nadir.

#### 1.2.3 Picosatellites: a quick review

As picosatellites, and specifically cubesats, evolved from larger spacecraft, the femtosatellite will evolve from the spacecraft that venture forth before it. The current state of the art in the smallest class of satellites will be reviewed to grow accustomed with the design philosophies relating to creating a low cost, lightweight satellite. For a complete treatment of picosatellites refer to (Alger, 2008)

Structurally cubesats are far more complicated than PCBsats. Typically the load bearing frame is comprised of aluminum, with several PCBs layered inside. A notable exception to this approach is CAPE-1 (University of Louisiana) which integrates the printed circuit boards with the structure. CAPE-1 was successfully launched on the 17<sup>th</sup> of April, 2007 and its beacon is listed as semi-operational as of April 2009. Cubesats do not have the mass or volume budgets to afford sealed enclosures for their electrical systems, and as a result the electrical systems are exposed to the vacuum of space, and possibly LEO atmosphere through the less than airtight gaps in the structure.

Attitude determination on cubesats is typically accomplished via magnetometers and sun sensors, when accomplished at all. Attitude control on cubesats is typically magnetic torquers

or passive. A notable exception to this paradigm is University of Toronto's CanX-2, with momentum wheels and cold gas thrusters.

Power subsystems on cubesats are often elaborate, leveraging maximum power point trackers, deployable solar cells, power control, battery management and enhanced telemetry points. This is likely due to the low amounts of power available in this form factor, as well as the availability of low cost COTS components to implement a variety of these features with little surface, mass and power consumption. Power storage on cubesats exclusively leverages lithium polymer batteries due to their huge mass advantage over NiCd and NiMH cells, as well as the simpler charging protocols.

#### **1.3 Design framework**

The scope of this work is to create and prototype a femtosatellite designed for low earth orbit operation. This femtosatellite will be capable of completing basic imaging missions, or missions with similar pointing requirements with payload masses not exceeding 25 grams. This will entail a completely custom design encompassing the following subsystems

- Command and data handling: This subsystem is responsible for the command and autonomous operation of the spacecraft, and the dispatching of ground commands at specific execution times.
- **Communication:** This subsystem is responsible for the radio data link between the satellite and ground station. Communication is required to be bi-directional between the satellite and ground.
- **Power:** The power subsystem manages energy accumulation from the solar arrays, battery charge condition and regulates battery voltage down to the bus voltage for reliable spacecraft operation.
- Attitude determination and control (ADCS): The ADCS estimates the attitude, or orientation with respect to the earth, of the spacecraft from onboard sensors and maintains required pointing through the actuators on the craft.

- **Payload:** While many payloads could be compatible with the femtosatellite, a specific payload subsystem has been created to take and store images of various visible objects.
- Structure and thermal: This subsystem carries the mechanical and thermal loads of the spacecraft during launch and orbit. Typically the structure is most important during launch, whereas the thermal subsystem is crucial during the satellites orbital lifetime.

#### **1.4 Contributions**

The present study contributes the following to the state of the art in femtosatellite design:

- i. The femtosatellite platform now has capacity for full attitude determination and control.
- ii. The femtosatellite platform now has a lightweight communications system capable of contacting a ground station from low earth orbit.

Derived from the aforementioned contributions, the following missions become feasible for the femtosatellite to perform.

- i. The femtosatellite can act as an inspector satellite to a co-orbiting satellite.
- ii. The femtosatellite can perform simple earth observation tasks requiring nadir pointing.
- iii. The femtosatellite can act as a store-and-forward communications satellite carrying short text messages.

#### 1.5 Thesis outline

Chapter 1 presents an introduction to femtosatellites and a literature review of studies to date, as well as works related to small satellite design. Chapter 2 covers the requirements used in the design of the spacecraft, and then the specifics of the design. Chapter 3 covers in detail

the attitude determination and control algorithms used in this design. Chapter 4 details the fabrication method of the satellite, test procedures and results of prototype testing. Finally chapter 5 draws conclusions from this work and offers further avenues of study to realize additional success in this area of research.

# Chapter 2

# **Requirements and Design**

#### 2.1 Introduction

In this chapter first the requirements for the femtosatellite and mission are presented, and then the subsystem design is explored in detail. While each subsystem is explored individually, many share hardware components with other subsystems. A hardware inventory and block diagram will be shown at the beginning of each subsystem description to give the element physical context.

#### 2.2 Requirements

#### 2.2.1 Mission requirements

			Verification
ID	Requirement	Origin	method
	The mission shall take pictures of arbitrary visible		
MIS01	objects.	Proposal	Design
MIS02	The mission shall be straightforward to launch.	Proposal	Design
MIS03	The mission should be reconfigurable.	Proposal	Design
MIS04	The mission should be low cost.	Proposal	Design
MIS05	The mission data shall be completely recorded.	Proposal	Design
MIS06	The mission should employ innovative methods.	Proposal	Design

#### **Table 2.2-1 Mission requirements**

### 2.2.2 System level requirements

			Verification
ID	Requirement	Origin	method
SYS01	System shall stabilize attitude on all three axes.	MIS01	Design
SYS02	System shall fit inside a standard cubesat.	MIS02	Design
SYS03	System shall have 25 grams of payload capacity.	MIS02&MIS03	Design
SYS04	System shall use COTS components where possible.	MIS04	Design
	System shall report basic and payload telemetry to		
SYS05	the ground station.	MIS05	Design
SYS06	System shall be low cost.	MIS04	Design
SYS07	System shall be robust.	Proposal	Design, Test
SYS08	System shall support various small science missions.	MIS03	Design
SYS09	System shall be implemented on a single PCB.	MIS04&MIS06	Design
SYS10	System shall use solder/ epoxy for mechanical joints.	MIS04&MIS06	Design
	The mission should observe standards and		
SYS11	paradigms in small/amateur satellite design.	MIS02	Design

#### Table 2.2-2 System requirements

#### 2.2.3 Command and data handling subsystem requirements

#### Table 2.2-3 C&DH requirements

			Verification
ID	Requirement	Origin	method
CDH01	Timekeeping shall be accurate to ±250ms.	SYS01&SYS08	Design, Test
CDH02	CDH shall maintain a 16 element instruction queue.	SYS08	Design
CDH03	CDH shall store telemetry for a minimum of one day.	MIS05&SYS07	Design
CDH04	CDH shall allow for a minimum of 1 reprogramming.	MIS03&SYS07	Design
CDH05	CDH shall use firmware watchdog timer.	SYS07	Design
CDH06	CDH shall employ a safe-hold mode.	SYS07	Design
CDH07	CDH shall maintain queue in non-volatile storage.	SYS07	Design
CDH08	CDH shall use only the top surface of the PCB.	SYS09&COM15	Design

# 2.2.4 Communication subsystem requirements

			Verification
ID	Requirement	Origin	method
COM01	COM shall transmit data at a minimum of 300 bps.	SYS11	Design
COM02	COM shall allow for a reconfigurable bit rate.	SYS07	Design
COM03	COM data rate shall default to 1200bps.	SYS11	Design
COM04	COM shall transmit a beacon.	MIS05&SYS11	Design
COM05	COM beacon shall be a maximum of 100 bytes.	MIS05	Design
	COM beacon shall be transmitted a minimum of once		
COM06	every 2 minutes.	SYS11	Design
	COM beacon shall be re-configurable from the		
COM07	ground station.	SYS11&SYS07	Design
COM08	COM beacon transmit power shall be +27dBm.	SYS05	Design
	COM beacon shall be disabled during ground station		
СОМ09	operations.		Design
	COM shall transmit with a maximum power in excess		
СОМ10	of +27dBm.	SYS07	Design, test
	COM transmit power shall be reconfigurable from		
СОМ11	ground.	SYS07	Design
COM12	COM shall radiate RF energy towards the earth.	SYS05	Design
	COM shall not use error correction, encryption or		
СОМ13	data whitening while beaconing.	SYS11&SYS07	Design
	COM shall allow for the enabling of error correction,		
	encryption or data whitening via ground station		
COM14	command.	SYS07	Design
	COM shall use the bottom of the PCB as a radio		
COM15	reflector.	SYS09&COM12	Design

#### Table 2.2-4 Communication requirements

#### 2.2.5 Power subsystem requirements

			Verification
ID	Requirement	Origin	method
	POW shall charge battery when battery is at correct		
POW01	temperature.	SYS07	Design
POW02	POW shall not attempt charge battery beyond 100%.	SYS07	Design
POW03	POW shall not allow battery to fully discharge.	SYS07	Design
POW04	POW shall supply $3.0V \pm 3\%$ to the system.	Proposal	Design, Test
POW05	POW shall supply up to 1A without fault.	Proposal	Design, Test
	POW shall supply energy to the system at a minimum		
POW06	efficiency of 90% from nominal to full load.	Proposal	Design, Test
	POW shall attempt maximum power point tracking on all		
POW07	solar arrays.	SYS07	Design
	Solar arrays shall perform at a minimum of 15% peak		
POW08	efficiency.	Proposal	Design
	POW shall not use the back of the PCB for any		
POW09	components aside from the solar array.	SYS09&COM15	Design

#### Table 2.2-5 Power requirements

#### 2.2.6 Attitude determination and control subsystem requirements

#### Table 2.2-6 ADCS requirements

			Verification
ID	Requirement	Origin	method
	ADC shall achieve a mean nadir pointing		Design,
ADC01	accuracy of 5 degrees.	SYS01&SYS05&SYS08	Simulation
	ADC actuators shall weigh no more than 15		
ADC02	grams.	Proposal	Design, Test
ADC03	ADC shall last the lifetime of the spacecraft.	SYS07	Design
ADC04	ADC shall allow for update of control algorithm.	SYS07&SYS08	Design
ADC05	ADC shall only use the top surface of the PCB.	SYS09&COM15	Design

#### 2.2.7 Structure and thermal subsystem requirements

Table 2.2-7 Structure and thermal requir	ements

			Verification
ID	Requirement	Origin	method
SCT01	SCT shall survive launch environment stresses.	SYS07	Design, Test
	SCT should insulate the electronics from LEO		
SCT02	atmosphere.	SYS07	Design
SCT03	Thermal control shall not use heaters.	Proposal	Design

#### 2.3 System block diagrams



Figure 2.3-1 System block diagram

The topology of the satellite system is illustrated in Figure 2.3-1. This satellite uses a star topology in both the data and power networks. This topology grows from the hardware interfaces, which lend themselves to the star topology while making a ring topology significantly more complicated. Figure 2.3-2 shows the corresponding hardware block diagram of the satellite system. The method of interface for each connection is detailed where applicable. The electrical subsystems only interface passively with the structure and thermal system of the satellite; hence these systems are omitted for clarity.



Figure 2.3-2 Hardware block diagram of satellite system


Figure 2.3-3 Prototype PCB art showing various subsystem components, body fixed co-ordinate frame denoted in the upper right hand corner

# 2.4 Command and data handling

Hardware utilized: cc2510 microprocessor

AT25DF641 flash memory



Figure 2.4-1 C&DH subsystem hardware block diagram

The command and data handling subsystem exists inside the cc2510 microprocessor. This microprocessor offers better cycle performance than the classic 8051 architecture due to the elimination of wasted bus states. The C&DH's responsibilities are to process ground station commands and execute them in a timely manner, while recording telemetry for later processing. All subsystems are connected directly to the C&DH in a star topology.

The 64 megabit flash memory allocated to the C&DH system is used to store telemetry items for later retrieval. The amount of flash memory required is determined by the telemetry string size, beacon frequency and storage interval. The requirements indicate that the telemetry string must be less than 100 bytes, broadcast at an interval of 2 minutes and stored for 1 day (1440 minutes) Hence the memory block allocated to the C&DH must be greater than

$$\frac{1440}{2} \times 100 = 72000 \tag{2.1}$$

As it is convenient to allocate memory in blocks with sizes of  $2^n$ , the base  $2^{17}$  (or 131072) bytes are allocated to the C&DH. The corresponding address vectors 0x000000h through 0x01FFFF are exclusively forbidden to the rest of the satellite subsystems. This is a total of 1.63% of the memory space available on the satellite.

While realtime operating systems are available for the 8051, the initial mission, with very well defined payload operations and timing requirements will not require one. The software operates in a single main loop, each time performing a number of housekeeping tasks, these tasks are:

- checking to see if the radio has received a valid ground packet
- checking to see if a payload instruction must be executed
- recording telemetry
- handing off control to the attitude/navigation subsystem
- handing off control to the power subsystem



#### Figure 2.4-2 CDH main loop firmware flow

Further, in parallel with the main loop, several interrupts will occur, these interrupts are: Highest priority - System clock Low priority - Radio module



Figure 2.4-3 CDH interrupt firmware flow

The system clock interrupt must be serviced with the highest priority to maintain good counting accuracy. If the free running counter overflows before the last timer interrupt has been served, the new interrupt will alias with the previous and a tick will be lost. All timekeeping on the satellite depends on this interrupt operating flawlessly. This interrupt has multiple initiation sources, however none of them will be used to avoid overloading the interrupt service routine.

The C&DH maintains three separate clocks: a second counter, a millisecond counter and an arbitrary timeout counter. The seconds counter is initiated during boot up, right after the deploy switch is released. The seconds counter begins at zero, counts seconds since boot and is never reset. The seconds count is maintained in a 32-bit unsigned integer which can accumulate a maximum of 4294967295 seconds before overflowing, or approximately 136

years. The milliseconds counter is initiated concurrently with the seconds counter, and accumulates every millisecond to a maximum count of 999. The counter is reset to zero at the edge of the thousandth tick, corresponding with the accumulation of another second. This counter serves to provide finer granularity for the seconds counter. Finally the timeout counter accrues ticks at the same rate and phase as the millisecond counter, however is free to be reset by user code. This timer is used for generating reliable multi-millisecond user delays without additional code fragments to handle overflow conditions. The timeout count is maintained in a 16-bit unsigned integer which can accumulate a maximum of 65.535 seconds before overflowing.

The radio is assigned to the lowest priority interrupt as it is the slowest data source on the satellite, and has extensive hardware buffering to ensure the integrity of the received data. In a usual radio exchange, the interrupt service routine will only be entered once to start the transaction, and once to complete it, with the direct memory access (DMA) controller and the radio first-in-fast-out (FIFO) buffer handling the intermediate steps. For these reasons the radio can tolerate some latency in interrupt processing.

Since interrupts can be dangerous to program flow and command execution latency, all efforts are made to reduce the amount of time from interrupt entry to interrupt exit. Furthermore, to harden the system against single event upsets, all masked interrupt sources will vector instead to the main loop entry point for satellite re-initialization. Given sufficient code space these interrupts could be allocated their own service routine which explicitly remasks the interrupt source and returns control to the main loop. Such a service routine can also be used to increment a special fault counter. The probability that a SEU would unmask an interrupt as opposed to corrupting less critical data is low given the relative memory space they occupy, however the occurrence of a spurious interrupt would be catastrophic to the stability of the system as a spurious interrupt allows for the execution of random bytes in memory.

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# 2.5 Communications subsystem

Hardware utilized: CC2510 microprocessor

T7026 Radio amplifier module

UPG2015 radio antenna switch

Antenna



#### Figure 2.5-1 Communication subsystem hardware block diagram

The communication system takes advantage of the embedded radio modem in the cc2510 microprocessor. This modem offers a full complement of features to make data transmission between the ground station and the satellite as robust as possible. The minimum signal required for a 1% bit error rate at 2400 bps is -103 dBm, or  $5*10^{-14}$  W. Data can be transmitted at variable rates to manage the ratio of bit energy to noise  $E_b / N_o$  for flawless communication. The radio supports automatic data whitening which ensures even power distribution across the expected spectrum. Forward error correction is supported in hardware, data can be packed with extra check bits to prevent single bit faults from corrupting transmitted data. Finally the module supports 128 bit AES encryption, which can be used to prevent unauthorized access to the most sensitive of commands the satellite must perform.

The radio modules responsibilities are exclusively the reception of commands from the ground station and their transfer to the C&DH's command buffer, and the transmission of the C&DH's telemetry or Payload data packets to the ground station. The radio requires very

little computational power from the cc2510 microprocessor, as the radio has associated hardware modules to streamline the movement of data to and from RAM. Radio interrupt design is covered in the command and data handling section of this chapter.

The default mode of the radio is receive mode, awaiting the reception of a valid preamble to a packet. In receive mode the T7026 amplifier module is put into receiver mode, activating its low noise amplifier (LNA). The antenna switch is configured to patch the LNA portion of the amplifier in between the cc2510 and the antenna, leaving the power amplifier open circuited at both ends. The LNA adds 16 dB of power intensity (gain) to the received signal to improve link budget performance.

When instructed by the C&DH the radio module will enter transmit mode. The T7026 amplifier will enter transmit mode, and the antenna switch will remove the LNA portion from the circuit and replace it with the power amplifier. The power amplifier adds up to 30dB of gain, to a maximum output power of 28 dBm, or 630 mW. This enables the femtosatellite to contact earth from LEO.

The antenna used is a planar patch antenna as described by (Tronquo 2006) or (Vermeeren et al, 2001). This style of antenna is flat, with radio emissions radiated from its broadside with circular polarization. The addition of a reflector attenuates emission in the normal direction of one antenna surface, while amplifying emission on the opposite surface. This antenna was chosen over more conventional dipole, monopole or designs primarily for space conservation and deployment simplification.

Table 2.5-1 Radio antenna comparison

Antenna style	Gain	mass	height	polarization	Deployment complexity
Dipole	6dbi	5~10g	22mm	Linear	high
patch	6dbi	~2g	2.54mm	Circular	low

The dipole antenna is heavier than expected because of the extra height associated with the dipole radiator. In order to keep the impedance high enough for effective coupling the

radiators must be 22mm above the reflector plane. Given that the desired height of the femtosatellite must be 10mm inside the launcher this implies that the antennas must be on some deployable mechanism with a high degree of mechanical and electrical (specifically radiofrequency) robustness. The patch antenna is small enough to simply use without designing for a deployable structure. The simplicity of using a patch antenna comes with a static 2.54mm height penalty, negligible mass penalty as the patch can be made from foil, and no electrical penalty. Circular polarization is a desired quality to avoid polarization attenuation of the received signal which is inherent in mismatched linear systems.



Figure 2.5-2 Radio patch antenna drawing (Tronquo 2006)

The choice of a directional antenna requires that the direction of radiation be coincident with the direction to the recipient of said radiation. This implies attitude control must point the antenna at the earth. The angular radii of the earth at orbital heights of 400 km and 800 km are (Larson and Wertz 1999)

$$\rho = \sin^{-1} \left( \frac{R_E}{R_E + H} \right) \tag{2.2}$$

Table 2.5-2 Angular radius of the Earth given various orbits

Orbital Height	ρ
400 km	70.22°
800 km	62.69°

As such the beam width of an antenna to illuminate all of the Earth from these orbits would be double the Earth angular radius, or 140.44° for the 400 km height and 125.38° for the 800 km height. The selected patch antenna offers a beam width of 120 deg before the antenna attenuates the transmitted signal.



Figure 2.5-3 Antenna radiation pattern, modified for clarity (Tronquo 2006)

The lack of full earth illumination means that the link on an overhead pass will be hindered during the opening and closing minute. Given that the radio module will be in low data rate beacon mode at the initiation of any contact window it is likely that the link budget margins can absorb this loss. The losses at the extreme edge of the beam width are manifested as gains in the center of the radiation pattern, with almost 9 dBi of gain directly overhead.

The link budget for this satellite has been designed around a 400 km circular orbit. Considering an overhead pass we can calculate the absolute maximum received signal strength and absolute minimum received signal strength and compare these values against the radios sensitivities to estimate the quality of our link. Because the final launch parameters for this satellite are open to some leeway, the link budget will also be calculated for an 800 km circular orbit, which is a typical sun synchronous orbit altitude.

The maximum distances from the ground station to the satellite are calculated below. (Larson and Wertz 1999) Assumed parameters are a minimum elevation angle  $\varepsilon_{\min}$  of 5 degrees, orbital altitude of 400 km and 800 km:

$$\sin \eta_{\text{max}} = \sin \rho \cos \varepsilon_{\text{min}}$$

$$\lambda_{\text{max}400km} = 90 - \varepsilon_{\text{min}} - \eta_{\text{max}}$$

$$D_{\text{max}} = R_E \frac{\sin \lambda_{\text{max}}}{\sin \eta_{\text{max}}}$$
(2.3)

Table 2.5-3 Maximum range for various orbits

Orbital height	$\eta_{ m max}$	$\lambda_{\max}$	$D_{\max}$
400 km	69.62°	15.37°	1804 km
800 km	62.26°	22.73°	2784 km

This distance is the source of the single greatest loss in the radio link: *space loss*. Space loss is calculated by (Larson and Wertz 1999)

$$L_s = 147.55 - 20\log S - 20\log f \tag{2.4}$$

Where  $L_s$  is the loss in decibels, S is the path length (or range) of the communication link in meters and f is the carrier frequency in Hz. Finally the received signal strength for each case can be calculated based on the link parameters. Figure 2.5-4 and Table 2.5-4 illustrate the best case, an overhead pass at a 400 km altitude; and worst case, the edge of the contact window at 800 km altitude; link budgets.



Figure 2.5-4 Link budget geometry

Overhead @ 400km height		Edge of window @ 800km height		
TX power	27 dBm	TX power	27 dBm	
Frequency	2450 MHz	Frequency	2450 MHz	
Range	400000 m	Range	2784000 m	
Satellite antenna gain	5 dBm	Satellite antenna gain	0 dBm	
Equivalent Radiated Power	32 dBm	Equivalent Radiated Power	27 dBm	
In watts	1584.89 mW	in watts	501.19 mW	
space loss	-152 dB	space loss	-169 dB	
ground antenna gain	30 dBi	ground antenna gain	30 dBi	
Ground LNA gain	16 dB	Ground LNA gain	16 dB	
Received Signal Strength	-74.27 dBm	Received Signal Strength	-96.13 dBm	
RSS in Watts	3.7×10 <sup>-11</sup> W	RSS in Watts	2.4×10 <sup>-13</sup> W	
Bit energy (Eb)	$1.5 \times 10^{-14}$ J	Bit energy (Eb)	$1 \times 10^{-16} J$	
System temperature	100000 K	System temperature	100000 K	
No	1.38×10 <sup>-18</sup> W/Hz	No	1.38×10 <sup>-18</sup> W/Hz	
Eb/No	40 dB	Eb/No	18 dB	

<b>Table 2.5-4</b>	Best	and	worst	case	link	budgets
--------------------	------	-----	-------	------	------	---------

To achieve a 1% bit error rate using FSK demodulation, the required ratio of bit energy to noise spectral density is 9 dB. Assuming a 25.3 dB system noise figure, the receiver sensitivity for various bitrates at 1% bit error rate is calculated in Table 2.5-5.

	Noise			Datasheet
Data rate (BPS)	density	Required Eb (J)	RSS (dBm)	RSS (dBm)
	(W/Hz)			
2400	1.38×10 <sup>-18</sup>	1.09572×10 <sup>-17</sup>	-105.8	-103
10000	1.38×10 <sup>-18</sup>	1.09572×10 <sup>-17</sup>	-99.6	-98
250000	1.38×10 <sup>-18</sup>	1.09572×10 <sup>-17</sup>	-85.6	-90
500000	1.38×10 <sup>-18</sup>	1.09572×10 <sup>-17</sup>	-82.6	-82

Table 2.5-5 Minimum Required signal strength for various bitrates

As a result we can calculate the link margin, which is the amount in excess of minimum required signal strength for a 1% bit error rate, for each datarate and range. This data is shown in Table 2.5-6.

Datarate/range	400km	800km	1804km	2784km
2.4kbps	28.7	22.7	10.6	6.9
10kbps	23.7	19.7	5.6	1.9
250kbps	15.7	9.7		
500kbps	7.7	1.7		

Table 2.5-6 Link margins for various ranges and datarates, all values in dBm.

Links with margins below 3db are not expected to function well due to implementation losses. Areas blacked out are calculated to be negative values, which represent received signal strengths below the minimum required to achieve 1% bit error rate. Overall the link performance appears excellent, offering the possibility of high data rates while overhead and the opportunity to monitor the satellite beacon towards the very edge of the contact window.

# 2.6 Attitude determination and control hardware

Hardware utilized: cc2510 microprocessor

PNI MS2100 magnetometer and Z axis sensor A, B and Z axis magnetic torquers 3 Allegro A3903 DC motor drivers XOR gate



Figure 2.6-1 Attitude determination and control hardware block diagram

The attitude determination and control system is designed to stabilize the satellite on all three axes and to provide proper pointing throughout the mission lifetime. The attitude determination system relies solely on the three axis magnetometer to make attitude measurements in conjunction with a Kalman filter. The attitude control system uses a combination of 3 magnetic torque actuators and passive drag stabilization to provide pointing of the antenna and payload to the nadir. For a detailed review of the attitude determination and control algorithms employed on this satellite please refer to chapter 3.

Magnetometer selection was driven by the need to reduce component count in interfacing with the cc2510 microprocessor. Magneto-resistive magnetometers are often complicated by

the addition of external amplifiers and magnetic set/reset circuitry which increases footprint and power requirements, as well as slowing design work. The MS2100 from PNI corporation integrates dual axis magneto-inductive compassing with a digital measurement ASIC, which has provisions for attaching a third out of plane sensor. This sensor uses only 6 wires to interface with the microprocessor (3 of which are bus wires) and consumes an order of magnitude less power than traditional magnetometers. The magneto-inductive design is inherently less prone to offset drift, improving the effectiveness of ground calibration.

Magnetometer data is compared to the IGRF ephemeris model of the geomagnetic field. The most current model is the IGRF2005, which is a 13<sup>th</sup> order spherical harmonic approximation of the geomagnetic field, with estimations of the secular variation components. Given a specific time and location the local magnetic intensity and direction can be determined. Orbital position to determine magnetic field will be determined using the SGP4 propagator from Celestrack and updated elements from the ground station.

Attitude control is accomplished through magnetic torque rods and drag stabilization. Drag stabilization works to restore the pitch and yaw angles with respect to the satellites velocity vector to zero, however this method offers no damping, especially since the satellite will be constructed to be as rigid as possible. In a 400 km orbit the peak torques from aerodynamic drag occur when the orientation about an axis is 90 degrees to the direction of travel. These torques are introduced by offsetting the center of mass of the satellite by 1cm from the center of pressure. The aerodynamic stabilization dictates the choice of the satellites co-ordinate system and resulting flying wedge configuration.

The magnetic torque rods are driven by the allegro A3903 DC motor driver, which is an intelligent H bridge. The motor driver IC is implemented in a 2mm by 2mm DFN-8 package, which is placed on the circuit board inside the Z-axis torque coil to take advantage of its EMI shielding effects. The XOR gate is used to create the complementary PWM signal to drive the A3903 ICs. The traces which carry the complementary PWM signal are paired to limit EMI.

The magnetic torque rods are the primary mass consumer of the ADACS subsystem and as such every effort is made to minimize their mass. A tradeoff exists between mass and power with magnetic torquer design, where for a given dipole moment a fixed number of amp-turns are required to create it. More wire windings allow for lower currents (and hence power) but add weight with each turn. Less windings make the torquer less power efficient and drive up energy requirements.

The magnetic torque actuators have been sized for a dipole moment of 0.01  $Amp \cdot turn \cdot m^2$ . This realizes a minimum peak torque of  $3.75 \cdot 10^{-7} Nm$ , which corresponds to an angular acceleration of  $0.72^{\circ}/\sec^2$ . This "minimum peak torque" occurs when the satellite is positioned at the magnetic equator, which exhibits the lowest magnetic field magnitude. Maximum peak torque occurs over the magnetic poles and has a magnitude of  $1.14 \cdot 10^{-6} Nm$ , corresponding to an angular acceleration of  $2.18^{\circ}/\sec^2$ , which is sufficient for an Earth observation satellite. The equation for calculating the dipole moment of a magnetic torque rod is given below.

$$\vec{M} = \frac{NIA}{\frac{1}{\mu_r} + N_d}$$
(2.5)

To realize a low mass, low power magnetic torque actuator a variation on the classic design is presented. The magnetic torque actuators mass is dependent on two items: the mass of its core, and the mass of its windings. Cores are selected based on their magnetic performance and geometry to optimize the dipole moment produced. Windings are selected based on their ability to carry current and proper resistance characteristics. Core optimization beyond using ferrite cores proves to be difficult as higher permeability magnetic alloys saturate quickly, limiting their usefulness as an electromagnet.

Given that we are limited to a MnZn ferrite core or an open core and the core geometry is fixed by the mission, which is true in this case as the femtosatellite severely constrains the available volume; we must find additional mass and power savings in the winding. In this case copper as a winding material was abandoned in favor of aluminum. The density of aluminum is around  $2700kg / m^3$ , as compared with coppers  $8900kg / m^3$ . The design current is only 50 mA at full moment, meaning that the higher resistivity of aluminum will not cause excessive power dissipation.

The two in plane magnetic torque rods are constructed identically. The core is 3mm diameter manganese zinc ferrite, 75mm long. The mass of the core is 2.8 grams. The demagnetization factor  $(N_d)$  of this geometry is estimated to be .01, the maximum allowable current into the torque rod is 50mA, and thus the required number of windings is

$$N = \frac{(\frac{1}{\mu_r} + N_d)M}{IA} = 284$$
(2.6)

Using aluminum American wire gauge #30 (AWG30 or 30AWG) wire the total winding mass is 0.8 grams, and the final mass of the torquer is 3.6 grams.

The one out of plane magnetic torque actuator (body Z axis torquer) is limited by the internal height of spacecraft. The internal gap between the board surface and the solar array is 5mm tall; hence the area must be increased to realize the required magnetic moment. An inner diameter of 40mm was selected for the coreless actuator to provide a good balance between surface area consumption and magnetic performance. The demagnetization factor for this configuration is tentatively estimated at 0.8, however demagnetization factors for hollow cylinders trends downwards for increasing ratios of inner radius to outer radius (Kobayashi 1996).

The resulting actuator having a dipole moment of .01 at a current of 50 milliamps is 48 mm in diameter, 5.52 grams in mass, comprised entirely of 286 turns of the same aluminum wire used in the previous torque rod construction. This mass is expected to be the maximum mass (due to uncertainty in demagnetization factor), and can likely be reduced after extensive testing.



Figure 2.6-2 Magnetic torque rod rendering

The total mass of the attitude control actuators is 12.85 grams, neglecting electronic support equipment, which is consumes negligible additional mass (sub gram) due to modern electronic packaging paradigms. The surface area consumption of the two in plane torquers is  $6cm^2$  cumulative, or 7.5% of the available. Surface area usage of the final open core torque actuator is low despite the large diameter, using only  $5.52cm^2$ , or 7.0%. The total area bounded by the open core actuator is  $12.5cm^2$ , but this area is not unusable. The power electronics which drive the magnetic torque actuators can be placed inside the Z axis torquer to make effective use of the space, while taking advantage of the conductive shield the aluminum windings will create to limit electromagnetic noise emissions to the rest of the craft. The Power subsystem section describes additional capitalization of this space and shielding effect for the power subsystem.

The inductance of the two ferrite rods can be found by the following formula:

$$L = \frac{\mu N^2 A}{l} = 8.6 \, mH \tag{2.7}$$

Given the inductance and the PWM frequency the ripple current can be calculated. The PWM frequency is chosen to be the highest possible with 8 bit precision, which is 101kHz. The ripple current in the torquer is then:

$$\frac{di}{dt} = \frac{V_L}{L} = \frac{3.0}{0.0086} = 349 \frac{A}{s}$$

$$\Delta I = \frac{\frac{di}{dt}}{f_{PWM}} = \frac{349}{101000} = 3.45 \, mA$$
(2.8)

# 2.7 Power subsystem

Hardware utilized: CC2510 microprocessor Battery LM2852 synchronous power converter LM3814 current sensors Sun-side Solar array Earth-side solar array



Figure 2.7-1 Power subsystem hardware block diagram

The electrical power subsystem is responsible for providing regulated power from the battery to the electrical loads of the satellite, and extracting the maximum amount of power from the solar arrays. Battery charging must also be controlled to maximize battery lifetime. The power converters are located inside the Z-axis magnetic torque coil to take advantage of the EMI shielding the windings offer, and the otherwise unusable space bounded by the torquer.



Figure 2.7-2 (a) PCB art of power subsystem and (b) photograph of assembled power subsystem illustrating magnetic torque coil space constraints

The Femtosatellite uses two solar arrays, one mounted to the bottom of the printed circuit board, at the surface of the radio reflector, and hence is referred to as the "earth side" array. This nomenclature stems from the fact that the antenna must always point towards to the earth to satisfy link requirements. Hence the second array, mounted on the scaffolding on the other side of the satellite faces the sun more often, and is referred to as the "sun side" array. The sun side array is the primary power collector, with a surface area of  $64 cm^2$ , the maximum energy input is 1.3 W. The array voltage is 4.4 V peak. Given that the desired attitude for earth observation and antenna pointing is aligned with the orbital frame, the orbit inclination will introduce cosine losses in this array seasonally.

The earth side solar array serves two functions, the first is to provide the satellite power while tumbling and before initial attitude capture. The second long term task is to harness solar energy from earths albedo, which can be as high as 35%, or  $478W/m^2$ . (Larson and Wertz, 1999) The size of this array is hindered by the communication antenna, and as such only covers  $39 cm^2$ . The maximum solar energy collected from this array is 280 mW. The array voltage is 4.4 V peak.

The maximum power point tracking converter has been implemented with a minimum of components, and a fail safe method of energy harvesting should the main processor fall offline. The structure of the converter is a boost converter.



Figure 2.7-3 MPPT boost converter structure

The structure of this converter allows for maximum energy extraction as long as the maximum power point of the array is below the battery voltage in addition to the diode forward voltage, which is the case when the array is experiencing low insolation, or is heated to a high temperature. In the case when the array maximum power point voltage exceeds the voltage of the battery and diode, the array will operate in direct energy transfer mode, which is expected to be less efficient. Given that the battery will only be discharged 10% per orbit, the minimum battery voltage is expected to be in the range of 3.6 to 3.7V, which is about the maximum power point of a room temperature solar array under maximum insolation, hence direct energy transfer in this case would be optimal regardless. In actual fact the majority of battery charging will occur just after the eclipse period when the battery is at optimal temperature to receive the charge, and has just finished its discharge cycle. This period of charging is characterized by exceptionally low insolation values, and the maximum power point voltage will be lower than the expected battery voltage. By the time the array is in full sunlight one quarter of the orbit will have passed, and the array will have attained a significant temperature rise over the optimal, lowering the maximum power point voltage as well. At full insolation the battery will have acquired enough energy to be fully charged, and will float at a voltage of around 4.1V.

The MPPT algorithm runs on the cc2510 processor, and uses the "perturb and observe" method of power point tracking. This algorithm is simple, but has been known to demonstrate poor tracking in rapidly varying insolation periods. (Femia 2005) Rapidly varying insolation is not expected however due to the lack of clouds in LEO. The operating point of the array is defined as the voltage the array operates at, and the resultant current at that voltage, in other words: the power output. The operating point is varied by adjusting the duty cycle of the boost converter to load down the array, or unload the array. The Perturb and Observe algorithm makes three power measurements around the current operating point of the array: one at exactly the operating point, one below the operating point (defined by the perturb parameter *delta*) and one above the operating point. The array operating point is then adjusted in the direction of maximum power, unless both perturbed measurements are lower than the current operating point, implying that the MPP has been achieved.



Figure 2.7-4 Solar array (a) power and (b) current characteristics (non-dimensional) given various insolation and temperature conditions. adapted from (Femia, 2005)

The 3 V regulator chosen for bus regulation is the LM2852-3.0 synchronous buck converter from National Semiconductor. This converter is attractive due to the low space requirements and high efficiency. A synchronous converter offers advantages over a simple freewheeling buck converter because the losses across the freewheeling diode are removed from the system. Instead a MOSFET is used as a switch to allow the converter to freewheel during the un-powered cycle.



Figure 2.7-5 (a) A simple buck converter and (b) A synchronous buck converter

The LM2852 provides this synchronous, high efficiency conversion autonomously, requiring only 5 external components. The final regulator circuit schematic is shown in Figure 2.7-6.



Figure 2.7-6 LM2852 power converter circuit diagram.



Figure 2.7-7 LM2852 efficiency curve (National Semiconductor, 2006)

As can bee seen in Figure 2.7-7 the efficiency of this power converter is greater than 91% for currents up to 1 amp. The maximum load is less than 0.7 A, and the nominal load is approximately 75 mA (both shown in table 2.6-1). The efficiency of the regulator is greater than 92% for this entire spectrum, satisfying the power regulation requirements.

Additionally the power regulator has a shutdown pin which can be put to good use. There may come a time when the satellite requires a full power cycle to be restored to proper operating condition. This enable pin should normally be in a logic high state to provide power to the satellite. As an extreme measure the fault determination and correction code on the microprocessor, or the ground station command, can assert this pin to a low state through a timer circuit to enforce a satellite wide power outage. After the timer expires the satellite will boot fresh and single event upsets in the cumulative ram of the satellite will be cleared.



Figure 2.7-8 Schematic of converter shutdown circuit.

After the assertion of the blackout pin, the blackout timer capacitor will be charged, and discharge through the blackout timer resistor, the resulting discharge curve is

$$V_{gate} = 3 - 3e^{-t/RC}$$
(2.9)

C is chosen to be 2uf to facilitate rapid charging (before the blackout disables the processor) and R is chosen to be 10Mohm to ensure a long term reset. The gate threshold voltage of the disable FET is 1.2V, or 40% of the initial capacitors charge voltage. The resulting blackout time is then

$$\ln(.6) = \frac{-t}{20} = 10.21s \tag{2.10}$$

which is sufficient to reset the entire satellite to its initial state.

The battery has been chosen to store 500mAh of energy at a nominal voltage of 3.7V. This battery is a single cell lithium polymer secondary cell type with a rectangular form factor. This battery chemistry undergoes irreversible changes when the cell is discharged below 2.8V, and the spacecrafts power management software will be programmed to shutdown the spacecraft before the battery undergoes this change. The maximum permissible voltage is 4.2V before irreversible and catastrophic failure occurs.

Lithium polymer battery chemistry is temperature sensitive. The impedance of the battery increases as the temperature decreases, and capacity will be perceived to decrease. At high temperatures the battery is capable of very high discharge currents, which can cause internal heating and eventual catastrophic failure. Typical safety cutoffs for lithium polymer batteries are around 90 degree Celsius. The femtosatellite will never draw more than 750mA from the battery, limiting the capacity for internal heating and allowing operation at higher temperatures without catastrophic failure.

The power budget was calculated using a reference orbit of 400 km mean altitude, circular, 45 degree inclination. Cosine losses have been calculated presuming the primary mission of nadir pointing is maintained, and these losses have been included in the "RMS duty" calculation. Eclipse periods have been estimated as half of the orbital period, despite being somewhat less. Overall Table 2.7-1 represents the absolute minimum power the satellite will be expected to operate on.

Electrical Loads					
	Voltage	Amperage	Max load	Duty cycle	Average load
ltem	(V)	(A)	(W)	(non-dim)	(W)
Microprocessor	3	0.02	0.06	1	0.06
Radio system RX	3	0.02	0.06	0.95	0.057
Radio system TX	4.2	0.5	2.1	0.05	0.105
Magnetic torque rods	3	0.15	0.45	0.01	0.0045
Sums		0.69	2.67		0.2265
		Solar S	upplies		
	Area	Efficiency	Max supply	RMS duty	Average supply
cell array	$(m^2)$	(non-dim)	(W)	(non-dim)	( <i>W</i> )
Upper (sunshine)	0.0064	0.15	1.309	0.225	0.295
Lower (earthshine)	0.0039	0.15	0.234	0.225	0.053
Sums			1.54344		0.347

Table 2.7-1 Power budget

The orbital average power consumption is shown to be 121 mW less than the orbital supply, resulting in a balanced budget with a 53% surplus. This surplus can be partially allocated to payload power requirements, and additional ground contact associated with payload operations.

The energy required during the eclipse period is 629J, this corresponds with 53mAh of battery capacity discharged during the eclipse period, or slightly less than 10%, meaning the battery operates at a very shallow depth of discharge, potentially improving the cycling performance by as much as a factor of 10.

# 2.8 Structure and thermal

Hardware Utilized: Printed circuit board Solar scaffolding Solar arrays





The structure of the femtosatellite is primarily FR4 fiberglass, which is the prime component of the Printed circuit board (PCB); which is used for mounting and operating the electric circuits of the satellite. The printed circuit board is sized to fit inside of a cubesat such that many could be stacked inside of a typical cubesat for transit and deployment in LEO. In addition to the main wafer structure, thin aluminum scaffolding is used to support the sun side solar array.

The printed circuit board is an ideal structural material for small satellites. FR4 has the same yield strength as aluminum, with half of the density. FR4 also has a lower magnetic permeability than aluminum (approaching that of free space) which reduces the systems impact on the magnetometer measurements. The satellite is designed to fit into a 90 mm by 90 mm by 10 mm rectangle, with notches in the corners to clear the side rails of the host vehicle. The PCB is shaped to exactly these dimensions to maximize electronics area.

The PCB topside is used for mounting electronics and their associated traces. The bottom is used for mounting solar panels to form the earth side array, and mounting the antenna. Additionally the copper ground plane on the backside of the array makes an efficient reflector of RF energy, meaning that the structure is acting as part of the antenna as well.

The aluminum scaffolding is designed to support the solar array, as well as to conduct energy gathered from the solar array to the main board. Both heat and electricity flow down the solar scaffolding. The solar scaffolding is constructed from 0.30 mm aluminum plate, and gains rigidity from the solar array it is soldered to.

Solder or epoxy is used for all mechanical joints. Small machine screws are typically used to assemble a small satellite, sometimes these screws are made from aluminum. Aluminum screws are very sensitive to stripping during installation, and steel screws have a large magnetic signature which makes them unattractive in such a small package. Solder and epoxy suffer from neither of these flaws, and avoid requiring holes in the PCB which complicate circuit routing.

Thermally, the satellite consists of three major nodes: the upper solar array, the PCB and lower array, and the battery. Each of these nodes has a high degree of internal heat conductivity, and some isolation from adjacent nodes.

	Mass
ltem	(grams)
РСВ	28
Battery	12
electronics	5
Solar array	10
Magnetic control rods	15
Patch antenna	5
Payload	25
Sum	100

# Table 2.8-1 Femtosatellite mass budget

# Table 2.8-2 Thermal node heat capacities

	Heat capacity
Node	(J/deg)
Sunside array	3.84
PCB	15.26
Battery	14.4

# Table 2.8-3 Thermal junctions between nodes

	Resistance
Junction	(deg/w)
Sunside to PCB	4.16
PCB to battery	0.38



Figure 2.8-2 Thermal model of satellite system

Aluminized Mylar foil (0.002 inch or 0.05mm thick) is epoxied around the perimeter of the satellite to reduce the exposure of the electronics to the LEO atmosphere. In addition the aluminized Mylar foil has an excellent capacity for rejecting radiant heat, and low thermal conductivity. The thermal properties of the aluminized Mylar imply that the spacecraft transfers negligible heat energy about its perimeter, simplifying analysis. The foil does not make an air tight seal around the satellite. Solar degradation of the aluminized Mylar material was put at less than 1% per year based on observations of the Echo 1 satellite (Ford, 1964). Atomic oxygen effects however are less forgiving, and the aluminum layer does not prevent the oxidization of the Mylar below (Banks et. Al., 2004). The expected lifetime of the Mylar in a 400km orbit is about one year.

DANKER TO THE ACKS

# Chapter 3 Attitude Determination and Control Algorithms

## 3.1 Introduction

The algorithms which govern the behavior of the attitude determination and control system are presented in this chapter. Both algorithms are dependent on the geomagnetic field for functionality. When using the geomagnetic field for attitude determination, the unfiltered attitude information is only 2 DOF, and the satellite attitude about the local magnetic field is unknown. Similarly with magnetic actuation, only torques that lie in the plane perpendicular to the local magnetic field are available.

Magnetic attitude determination is employed to reduce component count and thus hardware complexity. The corresponding increase in software complexity is preferred as mass and volume are more severely constrained than computing power and storage space. Magnetic attitude control is preferred over reaction wheels and thrusters due to the lack of moving parts, finite fuel constraints and volume constraints. A fully magnetic ADACS is possible given the nature of the Earth's magnetic field, which varies significantly in direction over the period of an orbit from the satellites perspective. This variation allows for full 3 DOF sensing and actuation over the period of an orbit, enabling system functionality.

This chapter presents a quick review of the international geomagnetic reference field to give better context to the space the algorithms function in. Attitude determination is detailed, followed by attitude control. Figure 2.3-3 shows the layout of the magnetic torquers and sensors used in this chapter.

Throughout this chapter a quaternion representation of spacecraft body to orbit orientation is used. This quaternion is always normalized, where

$$q^T q = 1 \tag{3.1}$$

and the expected stacking order of the orientation quaternion is

$$q = \begin{bmatrix} q_1 \\ q_2 \\ q_3 \\ q_4 \end{bmatrix} = \begin{bmatrix} \vec{\varepsilon} \\ \eta \end{bmatrix} = \begin{bmatrix} \varepsilon_x \\ \varepsilon_y \\ \varepsilon_z \\ \eta \end{bmatrix}$$
(3.2)

Euler angles in this chapter have been converted from quaternion representation in the 3-2-1 sequence as done in (Kuipers, 1998).

$$roll = \tan^{-1} \left( \frac{2\varepsilon_{y}\varepsilon_{z} + 2\eta\varepsilon_{x}}{2\eta^{2} + 2\varepsilon_{z}^{2} - 1} \right)$$
  

$$pitch = \sin^{-1} \left( -2\varepsilon_{x}\varepsilon_{z} - 2\eta\varepsilon_{y} \right)$$
  

$$yaw = \tan^{-1} \left( \frac{2\varepsilon_{x}\varepsilon_{y} + 2\eta\varepsilon_{z}}{2\eta^{2} + 2\varepsilon_{x}^{2} - 1} \right)$$
(3.3)

# 3.2 International geomagnetic reference field

Both the attitude determination and attitude control subsystems of this satellite depend exclusively on the Earth's magnetic field. The model which describes the expected magnitude and direction of this field at a given position and time is the International Geomagnetic Reference field. The IGRF2005 model will be reviewed as an introduction to the ADCS algorithms.

The IGRF2005 model represents the geomagnetic field as a  $13^{\text{th}}$  order spherical harmonic expansion. This model is in the  $10^{\text{th}}$  generation, and makes valid field predictions from 1900 to 2010. The magnetic field *B* at a particular point and time is given by the negative gradient of a scalar potential function

$$\bar{B} = -\nabla V \tag{3.4}$$

where the scalar potential function V is given by the spherical harmonic expansion

$$V(r,\theta,\phi,t) = R_{Earth} \sum_{n=1}^{k} \left[ \left( \frac{R_{Earth}}{r} \right)^{n+1} \sum_{m=0}^{n} \left[ \left( g_n^m(t) \cos(m\phi) + h_n^m(t) \sin(m\phi) \right) P_n^m(\theta) \right] \right]$$
(3.5)

where  $R_{Earth}$  is the earth equatorial radius,  $g_n^m$  and  $h_n^m$  are the Gaussian coefficients of degree n and order m,  $r, \theta, \phi$  are the geocentric radius, *co*elevation and east longitude from the prime meridian and  $P_n^m$  is the associated Legendre function of degree n and order m. The  $\overline{B}$  field in tangential co-ordinates can be calculated with (Makovec, 2001):

$$B_{r} = \frac{-dV}{dr} = \sum_{n=1}^{k} \left[ \left( \frac{R_{Earth}}{r} \right)^{n+2} (n+1) \sum_{m=0}^{n} \left[ \left( g^{n,m}(t) \cos(m\phi) + h^{n,m}(t) \sin(m\phi) \right) P^{n,m}(\theta) \right] \right]$$

$$B_{\theta} = \frac{-1}{r} \frac{-dV}{d\theta} = -\sum_{n=1}^{k} \left[ \left( \frac{R_{Earth}}{r} \right)^{n+2} \sum_{m=0}^{n} \left[ \left( g^{n,m}(t) \cos(m\phi) + h^{n,m}(t) \sin(m\phi) \right) \frac{dP^{n,m}(\theta)}{d\theta} \right] \right]$$

$$B_{\phi} = \frac{-1}{r \sin \theta} \frac{-dV}{d\phi} = \frac{-1}{\sin \theta} \sum_{n=1}^{k} \left[ \left( \frac{R_{Earth}}{r} \right)^{n+2} \sum_{m=0}^{n} \left[ m \left( g^{n,m}(t) \sin(m\phi) + h^{n,m}(t) \cos(m\phi) \right) P^{n,m}(\theta) \right] \right]$$
(3.6)

where

$$g^{n,m} = S_{n,m} g_n^m$$

$$h^{n,m} = S_{n,m} h_n^m$$

$$S_{n,m} = \frac{(2n-1)!!}{(n-m)!} \sqrt{\frac{(2-\delta_m^0)(n-m)!}{(n+m)!}}$$

$$\delta_j^i = \begin{cases} 1 & i=j\\ 0 & i\neq j \end{cases}$$

$$P^{0,0} = 1$$

$$P^{n,n} = \sin \theta P^{n-1,n-1}$$

$$P^{n,m} = \cos \theta P^{n-1,m} - K^{n,m} P^{n-2,m}$$

$$K^{n,m} = \begin{cases} \frac{(n-1)^2 - m^2}{(2n-1)(2n-3)} & n > 1\\ 0 & n = 1 \end{cases}$$
(3.7)

# 3.3 Attitude dynamics

The co-ordinate frames used in this chapter are the body fixed co-ordinate frame  $F_B$ , the orbital co-ordinate frame  $F_o$  and the inertial co-ordinate frame  $F_I$ . All of these co-ordinate frames are right handed systems. For the purpose of this study the Earth centered inertial co-ordinate frame is considered sufficiently inertial, where Z lies along the Earth's spin axis, and X points towards the Vernal Equinox. The orbital co-ordinate frame X is in the direction of the along track velocity and Z points towards the Earth's center of mass. Finally the body fixed co-ordinate frame represents the spacecrafts own co-ordinate system, with the origin at the satellites center of mass.



Figure 3.3-1 Co-ordinate frames used in this chapter
The system dynamic equations can be written as follows:

$$\dot{\vec{\omega}} = I^{-1}(\vec{\tau} - \vec{\omega} \times I\vec{\omega}) \tag{3.8}$$

$$\vec{\omega} = \begin{bmatrix} \omega_x \\ \omega_y \\ \omega_z \end{bmatrix}$$
(3.9)

$$\dot{q} = \frac{1}{2} \begin{bmatrix} 0 & \omega_z & -\omega_y & \omega_x \\ -\omega_z & 0 & \omega_x & \omega_y \\ \omega_y & -\omega_x & 0 & \omega_z \\ -\omega_x & -\omega_y & -\omega_z & 0 \end{bmatrix} q$$
(3.10)

$$\vec{\tau} = \vec{\tau}_{drag} + \vec{\tau}_{dist} + M \times B \tag{3.11}$$

Where  $\bar{\omega}$  is the body frame angular velocity with respect to the inertial frame, I is the satellite inertia tensor, q is the quaternion which represents the orientation from the orbital co-ordinate frame to the body fixed co-ordinate frame and  $\bar{\tau}$  is the vector sum of external torques on the system in the body frame.  $\tau$  comprises the aerodynamic drag component  $\tau_{drag}$ , and the disturbance torques  $\tau_{dist}$ , and the torque due to the applied magnetic dipole  $\bar{M}$  and the Earth's magnetic field  $\bar{B}$ .

The orbital co-ordinate frame rotates about the pitch axis at an angular velocity of

$$\vec{\Omega} = \begin{bmatrix} 0\\ -2\pi\\ P\\ 0 \end{bmatrix}$$
(3.12)

where P is the orbital period, in seconds. This quantity is expressed in the orbital co-ordinate frame.

The drag torque is the sum of the drag torques from each face of the satellite exposed to the LEO atmosphere in the direction of the satellites velocity. In general, the drag force experienced by an arbitrary face of the satellite can be modeled in the body frame as follows

$$\vec{F}_{n} = \begin{cases} (-\hat{V}) \frac{1}{2} \rho V^{2} C_{d} (\vec{A}_{n} \cdot \hat{V}) & \vec{A}_{n} \cdot \hat{V} > 0 \\ \vec{0} & \vec{A}_{n} \cdot \hat{V} \le 0 \end{cases}$$
(3.13)

where  $\hat{V}$  is the unit vector in the direction of the satellites motion,  $\rho$  the atmospheric density, V the along track scalar velocity of the satellite,  $C_d$  the drag coefficient and  $\bar{A}$  the vector area of the face. The product  $\bar{A}_n \cdot \hat{V}$  accounts for the contribution of a particular face to the cross sectional area of the satellite, but only if this product is positive - a negative result indicates that the surface is not forward-facing. As such the torque due to drag acting on the satellite can be computed as

$$\bar{\tau}_{drag} = (C_p(n) - C_m) \times \sum \vec{F}_n \tag{3.14}$$

where  $C_p(n)$  is the respective center of pressure of the surface under evaluation,  $C_m$  is the centre of mass of the satellite and  $F_n$  is calculated from equation(3.13).

## 3.4 Attitude determination

An extended Kalman filter (EKF) is employed to estimate the satellite attitude and body rates using the measured geomagnetic field unit vector. The filter design employed is an adapted version of (Psiaki, 1990). This filter uses the difference between the propagated and measured magnetic field vectors to rotate the attitude estimate about the 2 degrees of freedom the magnetic measurement constrains. Given sufficient magnetic vector variance over an orbital period, the filter converges on an attitude estimate.

#### 3.4.1 Measurement model

The measurement used is the output of the magnetometer. The geomagnetic field is sensed along the three body fixed axis of the satellite, and can be defined as

$$\bar{B}_{meas} = A_{bi}\bar{B}_{eci} \tag{3.15}$$

Where  $\bar{B}_{meas}$  and  $\bar{B}_{eci}$  is the geomagnetic field in the body fixed and Earth centered inertial frames respectively, and  $A_{bi}$  is the co-ordinate transformation matrix given by

$$A_{bi} = \begin{bmatrix} q_1^2 - q_2^2 - q_3^2 + q_4^2 & 2(q_1q_2 + q_3q_4) & 2(q_1q_3 - q_2q_4) \\ 2(q_1q_2 - q_3q_4) & -q_1^2 + q_2^2 - q_3^2 + q_4^2 & 2(q_2q_3 + q_1q_4) \\ 2(q_1q_3 + q_2q_4) & 2(q_2q_3 - q_1q_4) & -q_1^2 - q_2^2 + q_3^2 + q_4^2 \end{bmatrix}$$
(3.16)

Where  $q_n$  is the quaternion which represents the orientation from the Earth centered inertial co-ordinate frame to the body fixed co-ordinate frame.

## 3.4.2 Linearized system model for determination

The attitude dynamics are linearized about the nominal attitude

$$\Delta \dot{\omega} = I^{-1} \left[ \Delta \tau - \Delta \omega \times I \Omega - \Omega \times I \Delta \omega \right]$$
(3.17)

However, the skew symmetric of a vector multiplied by another vector is equivalent to a cross product, therefore the following is true

$$\Delta \dot{\omega} = I^{-1} \left[ \Delta \tau + I \Omega \times \Delta \omega - \Omega \times I \Delta \omega \right]$$
  
=  $I^{-1} \left[ \Delta \tau + (I \tilde{\Omega}) \Delta \omega - (\tilde{\Omega} I) \Delta \omega \right]$   
=  $I^{-1} \left[ \Delta \tau + ((I \tilde{\Omega}) - (\tilde{\Omega} I)) \Delta \omega \right]$   
=  $I^{-1} \left( (I \tilde{\Omega}) - (\tilde{\Omega} I) \right) \Delta \omega + I^{-1} \Delta \tau$  (3.18)

Where  $\tilde{\Omega}$  is the skew symmetric form of the orbital frame angular velocity with respect to the inertial frame. This formulation of the linearized attitude dynamics lends itself well to discretization. The rest of the attitude dynamics are linearized similarly to (Psiaki, 1990) as follows

$$\Delta \dot{q} = \frac{1}{2} \Delta \omega \tag{3.19}$$

$$\Delta \tau = \Delta \tau_{drag} + \Delta \tau_{dist} + \Delta (\vec{M} \times \vec{B})$$
(3.20)

$$\vec{B}_{meas} = \vec{B}_{orb} - 2\Delta \tilde{q} \vec{B}_{orb}$$
(3.21)

and it is assumed  $\dot{\tau}_{dist} = 0$ , the quaternion, when linearized about small angles, experiences negligible change in the scalar component, and the scalar component is thus dropped from the linearized state vector. The linear state vector used to establish the linear state propagation matrix is

$$\Delta \chi = \begin{bmatrix} \Delta \omega \\ \Delta q_{1,2,3} \\ \Delta \tau_{dist} \end{bmatrix}$$
(3.22)

The 9x9 linear state propagation matrix can then be written as a 3x3 matrix of 3x3 matricies as follows

$$F = \begin{bmatrix} I^{-1}(I\tilde{\Omega} - \tilde{\Omega}I) & 0 & I^{-1} \\ \begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{2} \end{bmatrix} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
(3.23)

The linear state vector is not used in the propagation of the Extended Kalman filter.

#### 3.4.3 Kalman filter structure

The Kalman filter is a recursive filter, where the output is dependant only on the propagated state vector X, propagated error covariance P and the latest measurement  $\overline{B}$ . Figure 3.4-1 illustrates the overall structure of the filter. This particular implementation of the extended Kalman filter uses a modified innovation vector, and quaternion multiplication instead of addition in the update phase. Throughout this section a subscript of k indicates a value calculated in the previous iteration of the filter, a subscript of k+1 indicates a value calculated in the current iteration of the filter, a superscript of - indicates a value calculated before the current iteration update phase of the filter, and a superscript of + indicates a value calculated after the current iteration update phase of the filter.



Figure 3.4-1 Kalman filter block diagram

**Propagation phase** 

State propagation is performed via the standard nonlinear equations of rigid body motion covered in equations (3.8) through (3.11). The state vector used is then

$$\hat{X} = \begin{bmatrix} \hat{\omega} \\ \hat{q} \\ \hat{\tau} \end{bmatrix}$$
(3.24)

where the ( $^{}$ ) embellishment indicates that the parameter is an estimate. Propagation of the error covariance matrix *P* cannot be performed with the nonlinear equations and must use the linear state propagation matrix *F* as follows

$$P_{k+1}^{-} = F P_{k}^{-} F^{T} + Q \tag{3.25}$$

where Q is the process noise.

## Update phase

The innovation vector is unique to this filter, and employs the unit vector cross product of the measured and pre-update estimated magnetic field.

$$V = \frac{B_{meas} \times \hat{B}^-}{|B_{meas}||\hat{B}^-|}$$
(3.26)

Due to the unique innovation vector, the observation matrix is calculated in a unique manner as well and is given by

$$H = \frac{-dV}{d\Delta X} = \begin{bmatrix} 0 & \frac{-2\hat{B}^{-}B_{meas}^{T}}{|\hat{B}^{-}||B_{meas}|} & 0 \end{bmatrix}$$
(3.27)

The gain calculation stage of the filter is the standard implementation, and is performed by

$$K = \begin{bmatrix} K_{\omega} \\ K_{q} \\ K_{r} \end{bmatrix} = P_{k+1}^{-} H^{T} \begin{bmatrix} R + HP_{k+1}^{-} H^{T} \end{bmatrix}^{-1}$$
(3.28)

However the state update must be split to account for the non-standard innovation. While angular velocity and disturbance torque estimates are performed in the usual manner, the quaternion update employs quaternion multiplication

$$\omega_{k+1}^{+} = \omega_{k+1}^{-} + K_{\omega} V \tag{3.29}$$

$$\tau_{k+1}^{+} = \tau_{k+1}^{-} + K_{\tau} V \tag{3.30}$$

$$q_{k+1}^{+} = q_{k+1}^{+} \bullet \begin{bmatrix} KV \\ \sqrt{1 - (KV)^{2}} \end{bmatrix}$$
(3.31)

Where the (•) operator is used to represent the quaternion multiplication sequence of operations. The estimated state vector  $\begin{bmatrix} \omega_{k+1}^+ & q_{k+1}^+ \end{bmatrix}^T$  is now ready to be passed off to the attitude control system.

# 3.5 Attitude control

The attitude control system makes use of three state feedback controllers to control the roll, pitch and yaw axis. The axis are treated as uncoupled for the design of the controller, hence axial coupling behaves as a small disturbance to the linear system. Input linearization is used to remove some of the restorative torque of aerodynamic drag on the pitch axis. The control law used is from (Wie, 2008), a quaternion regulator:

$$\vec{u} = -k_p \operatorname{sgn}(\eta)\vec{\varepsilon} - k_d(\vec{\omega} - \bar{\Omega}) \tag{3.32}$$

Where  $\bar{\omega}$  is the angular velocity of the body fixed co-ordinate frame,  $\bar{\Omega}$  is the angular velocity of the orbital co-ordinate frame,  $\eta$  and  $\bar{\varepsilon}$  and the quaternion real and imaginary components (respectively),  $k_p$  is a 3x3 diagonal matrix of proportional gains and  $k_d$  is a 3x3 diagonal matrix of derivative gains. The  $\bar{\omega}$ ,  $\eta$  and  $\bar{\varepsilon}$  parameters are estimated by the Kalman filter.

#### 3.5.1 Linearized system model for control

The parameters used for linearization are

$$q_{o} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}, \omega_{o} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$
$$I = \begin{bmatrix} I_{x} & 0 & 0 \\ 0 & I_{y} & 0 \\ 0 & 0 & I_{z} \end{bmatrix}$$

Considering only a single (arbitrary) axis case the linearized system equations of motion from (3.8) to (3.10) become

$$\dot{\omega}_j = I_j^{-1} \tau_j \tag{3.33}$$

$$\varepsilon_j = \frac{1}{2}\omega_j \tag{3.34}$$

where  $j \in (x, y, z)$ , hence the coupling between the axes is neglected. The three axes can now be treated as three separate linear systems for the purposes of calculating control gains.

#### 3.5.2 Calculating control gains

Using a negative state feedback controller on the system defined by equations (3.33) and (3.34), the system is represented by the state space equation (3.36)

$$X = AX - BKX$$
  

$$\dot{X} = (A - BK)X$$
(3.35)

$$\begin{bmatrix} \dot{\varepsilon}_{j} \\ \dot{\omega}_{j} \end{bmatrix} = \begin{bmatrix} 0 & \frac{1}{2} \\ -k_{p,j}I_{j}^{-1} & -k_{d,j}I_{j}^{-1} \end{bmatrix} \begin{bmatrix} \varepsilon_{j} \\ \omega_{j} \end{bmatrix}$$
(3.36)

This linearized system lends itself to pole placement in the usual manner. The eigenvalues of the state matrix are the system poles. Solving algebraically

$$\det(SI - A) = \det \begin{bmatrix} S & \frac{-1}{2} \\ k_{p,j}I_j^{-1} & S + k_{d,j}I_j^{-1} \end{bmatrix} = S^2 + k_{d,j}I_j^{-1}S + k_{p,j}I_j^{-1} = 0$$
(3.37)

This is the characteristic equation of the closed loop response of the linear system. This can be equated to the classical second order system equation

$$S^{2} + k_{d,j}I_{j}^{-1}S + k_{p,j}I_{j}^{-1} = S^{2} + 2\zeta\omega_{n}S + \omega_{n}^{2} = 0$$
(3.38)

$$k_{p,j} = 2\omega_n^2 I_j \tag{3.39}$$

$$k_{d,j} = 2\zeta \omega_n I_j \tag{3.40}$$

 $\zeta$  in this case is chosen to equal 1. The 2% settling time is chosen to be 180 seconds to prevent the satellite from slewing too fast.  $\omega_n$  can then be calculated from the settling time

$$\omega_n = \frac{4}{t_s \zeta} \tag{3.41}$$

Control gains for the controller from equation (3.32) are calculated for each axis from equations (3.39) and (3.40), then placed in their respective gain matrices as follows

$$k_{p} = \begin{bmatrix} k_{p,x} & 0 & 0 \\ 0 & k_{p,y} & 0 \\ 0 & 0 & k_{p,z} \end{bmatrix}, k_{d} = \begin{bmatrix} k_{d,x} & 0 & 0 \\ 0 & k_{d,y} & 0 \\ 0 & 0 & k_{d,z} \end{bmatrix}$$
(3.42)

## 3.5.3 Aerodynamic disturbance rejection

Aerodynamic drag torque acts to create stiffness about the pitch and yaw axes, quite significantly so on the pitch axis. By subtracting the aerodynamic drag torque from the control effort the system tracking is better maintained than treating aerodynamic drag torque as a disturbance. The final control law is presented below

$$u = -k_p \operatorname{sgn}(\eta) \vec{\varepsilon} - k_d (\vec{\omega} - \vec{\Omega}) - \vec{\tau}_{drag}$$
(3.43)

#### 3.5.4 Magnetic actuator mapping

To apply the desired control torques to the system, they must be transformed into a magnetic moment. This is done using the rule proposed by (Sidi 1997). The magnetic dipole moment is calculated from the desired control torque by

$$\bar{M} = \frac{\bar{B} \times \bar{u}}{\bar{B}\bar{B}^T} \tag{3.44}$$

Where  $\overline{M}$  is the dipole moment vector,  $\overline{B}$  is the Earths magnetic field in the body frame, and  $\overline{u}$  is the desired control torque. After mapping, torque components which act around the local magnetic field direction are lost. Here aerodynamic drag torque assists the controller substantially about pitch and yaw when actuation about these axes is compromised by enforcing stiffness and in doing so, transferring energy to the other axes through the coupling in the equations of motion.

# 3.5.5 Numerical Simulation

To validate the control design, numerical simulations were performed on two system models. The parameters and initial conditions used in these simulations are detailed in Table 3.5-1.

Parameter	Value		
<i>I</i> Satellite inertia tensor	$\begin{bmatrix} 2.794 & .038 & .104 \\ .038 & 3.098 & .009 \\ .104 & .009 & 5.863 \end{bmatrix} \times 10^{-5} \ kgm^2$		
$k_p$ Proportional gain coefficients	$\begin{bmatrix} 2.639 & 0 & 0 \\ 0 & 2.927 & 0 \\ 0 & 0 & 5.539 \end{bmatrix} \times 10^{-8}$		
$k_d$ Derivative gain coefficients	$\begin{bmatrix} 1.214 & 0 & 0 \\ 0 & 1.347 & 0 \\ 0 & 0 & 2.548 \end{bmatrix} \times 10^{-6}$		
$q = \begin{bmatrix} \overline{\varepsilon} & \eta \end{bmatrix}^T$ Quaternion representation of initial orientation error	$\begin{bmatrix} .1483 & .1482 & .1483 & .9664 \end{bmatrix}^T$		
Angular velocity vector ( $\omega$ )	$\begin{bmatrix} 0 & 0 \end{bmatrix}$ rad / s		
Right ascension of ascending node ( $\Omega$ )	0 <i>rad</i>		
Orbital radius ( $r_o$ )	6778000 m		
Orbit eccentricity (e)	0		
Orbital period (P)	5553 s		
Orbital inclination (i)	0 <i>rad</i>		
Argument of latitude (U)	0 rad		
Atmospheric density ( $\rho$ )	$2.72 \cdot 10^{-12} \ kg \ / \ m^3$		
IGRF/WMM coefficient order ( $k$ )	12		
Date	15 July 2009		
Sidereal Time	0 <i>rad</i>		

Table 3.5-1 Numerical simulation parameters and initial conditions

Figure 3.5-1 to Figure 3.5-4 illustrate the response of a hypothetical satellite system to this controller. This satellite system assumes torque is available about all axis, and regulates its attitude with respect to the non-rotating inertial frame. No disturbances are assumed. The system is stabilized to zero angular error in about 400 seconds, which represents about  $1/10^{\text{th}}$  of an orbit. The magnitudes of the angular velocities are below 0.14 deg/s.



Figure 3.5-1 Euler angles for fully actuated satellite during stabilization



Figure 3.5-2 Angular velocity of fully actuated satellite during stabilization



Figure 3.5-3 Control torque for fully actuated satellite to achieve stabilization



Figure 3.5-4 Quaternion imaginary components for fully actuated satellite during attitude stabilization

The plots below illustrate the controller performance in a 400km earth orbit of 45 degree inclination. Initial attitude errors are about 20 degrees roll, 15 degrees pitch and 20 degrees yaw. Figure 3.5-5 shows the Euler angle history for the satellite without any control. Clearly evident is the stiffness about pitch and yaw as a result of aerodynamic drag. The roll axis is subject only to gravity gradient and coupling torques which are several orders of magnitude smaller. As such the roll axis limit cycle is not visible on the timescale presented.



Figure 3.5-5 Euler angles for uncontrolled satellite in Earth orbit

Figure 3.5-6 to Figure 3.5-12 demonstrate the performance of the above control law and magnetic mapping law on the simulated satellite system in Earth orbit. Here the controller is applied to regulate the attitude of the satellite such that it aligns itself with the orbital frame. This attitude is desired to accomplish various Nadir pointing missions, and to maintain the link budget. Figure 3.5-12 in particular shows the magnitude of the nadir pointing error vector, which is particularly important to earth observation applications. Nadir pointing error is limited to 1 degree after only 2 orbits and remains bounded for the duration of the simulation.



Figure 3.5-6 Quaternion imaginary components for Earth orbiting satellite



Figure 3.5-7 Euler angles for Earth orbiting satellite



Figure 3.5-8 Desired control torque for Earth orbiting satellite



Figure 3.5-9 Realized magnetic control torque for Earth orbiting satellite

The magnetic mapping law has the capacity to vastly corrupt the desired control torque given sub optimal magnetic field vectors. Figure 3.5-10 shows a detailed view of the desired versus realized control torques during the first half orbit (2776 seconds) of simulation. Note the capacity for sign inversion of the desired torque. A zero reference line has been added to this plot to assist with visualization.



Figure 3.5-10 Desired and realized torque plot for the first half orbit of simulation



Figure 3.5-11 Applied dipole moment and geomagnetic field in body fixed frame



Figure 3.5-12 Magnitude of nadir pointing error



# Chapter 4 Fabrication and Testing

# 4.1 Introduction

During the latter half of this study a prototype femtosatellite was fabricated. This chapter covers the assembly instructions for the prototype, as well as baseline test procedures to verify system functionality. Finally simulation and test results measured from the prototype hardware are presented.

# 4.2 Assembly

This section details the correct method to assemble the femtosatellite. After the completion of a subsystem, immediately follow the corresponding test procedure in the following section. All instructions pertain to version 1.0 of the prototype board, which contains no version marking information. Subsequent femtosatellites will indicate their version number on both sides of the PCB.

All soldering shall be done with tin-lead solder and in accordance with NASA Technical standard 8739.3 "Soldered Electrical Connections". The satellite shall never be assembled with power applied. A pre-heater shall be used to ramp up board temperature at a rate of no more than 2 degrees Celsius per second. Moisture sensitive components must be baked if original packaging is opened for more than 24 hours, or if humidity papers indicate so. The satellite must be baked before any rework can be performed.

# 4.2.1 Power subsystem

Beginning with a bare femtosatellite PCB, assemble the following power components in the order listed.

Schematic name	Manufacturer PN	Description	Solder method
REG	LM2852YMXA-3.0	3.0V regulator	REFLOW
Lout	b82462-g4223-M	22uH inductor	IRON
Cout	TPSC107K006R0150	100uf capacitor	IRON
Css	generic 0402 ceramic	2.7nf slow start cap	IRON
Cf	generic 0402 ceramic	1uf filter	IRON
Rf	generic 0402 thick film	10ohm filter	IRON
DEP_SW	JSM08022SAQNL	deploy switch NC	IRON
CSB	LM3814M-1.0	battery current sense	IRON
C1,C2	generic 0402 ceramic	0.1uf capacitor	IRON
R3	generic 0402 thick film	10kohm pullup	IRON

Table 4.2-1	Components	for	assembly	in	step	1
			eroo eranory			-

After assembly there are enough components placed to test the most basic function of the power subsystem. Please refer to "power subsystem initial test" test procedure before continuing. Component damage can occur if the power subsystem is not tested at this point.

Continuing the power subsystem assembly, place the following components in the order listed in Table 4.2-2.

Schematic name	Manufacturer PN	Description	Solder method
CSA1	LM3814M-1.0	battery current sense	IRON
C3,C4	generic 0402 ceramic	0.1uf capacitor	IRON
R2	generic 0402 thick film	10kohm pullup	IRON
CSA2	LM3814M-1.0	battery current sense	IRON
C5,C6	generic 0402 ceramic	0.1uf capacitor	IRON
R1	generic 0402 thick film	10kohm pullup	IRON

Table 4.2-2 Components for assembly in step 2

CS1,CS2,CBAT	TPSC107K006R0150	100uf capacitor	IRON
LS1,LS2	ELL-CTV102M	1mH inductor	IRON
QS1,QS2	IRLML2502PbF	NFET	IRON
D1	20CJQ030	Dual diode	IRON
CB2	generic 0402 ceramic	0.1uf capacitor	IRON
R8	generic 0402 thick film	1kohm resistor	IRON
R9	generic 0402 thick film	2kohm resistor	IRON

Table 4.2-2 Components for assembly in step 2(Contd.)

This completes the power system peripheral components. The last two items that form the power system, the cc2510f32 processor and battery, will be addressed later.

## 4.2.2 Command and data handling

With a femtosatellite PCB that has the power subsystem assembled and verified for Power "initial test" functionality, continue to assemble the following components in order listed.

Schematic name	Manufacturer PN	Description	Solder method
CC2510	cc2510f32	Microprocessor/radio	REFLOW
Cd	generic 0402 ceramic	1uf decoupling	IRON
CDn	generic 0402 ceramic	.1uf decoupling	IRON
Cser	generic 0402 ceramic	10pf decoupling	IRON
Rbias	generic 0402 thick film	56k resistor	IRON
XTAL	CSX-325T	26MHz TCXO	IRON
Rrst	generic 0402 thick film	10k resistor	IRON
Crst	generic 0402 ceramic	.1uf decoupling	IRON
DEBUG	generic .1" header	2 rows of 5 pins each	IRON
flash	at25df641	32MBit flash memory	IRON

Table 4.2-3 Components for assembly in step 3

After assembly basic processor functionality should be verified. Please refer to "Command and data handling initial test" in testing procedures. This test is not required to prevent damage but will greatly speed debugging if a fault has occurred at this stage.

# 4.2.3 Communication

Continue assembly on a PCB populated with the power and command and data handling systems, which have been verified for Power and C&DH "initial test" functionality. Assemble the following components in order listed.

Schematic name	Manufacturer PN	Description	Solder method
AMP	T7026	RF frontend	REFLOW
SW1,SW2	UPG2015	RF switch	REFLOW
C231,C241	RF grade 0402 ceramic	100pf	REFLOW
C232,C242	RF grade 0402 ceramic	1.0pf	REFLOW
C233	RF grade 0402 ceramic	1.8pf	REFLOW
C234	RF grade 0402 ceramic	1.5pf	REFLOW
L231,L232,L241	RF grade 0402	1.2nH	REFLOW
CSW1,CSW2	RF grade 0402 ceramic	56pf	REFLOW
Camp1,Camp5	RF grade 0402 ceramic	2.7pf	REFLOW
Camp2	RF grade 0402 ceramic	2.2pf	REFLOW
Camp3,Camp4	RF grade 0402 ceramic	2.0pf	REFLOW
Lamp1	RF grade 0402	3.9nH	REFLOW
Lamp2	RF grade 0402	15nH	REFLOW
C9	RF grade 0402 ceramic	1.8pf	REFLOW
C10	RF grade 0402 ceramic	3.9pf	REFLOW
C7	generic 0402 ceramic	.1uf	REFLOW
C8	RF grade 0402 ceramic	100pf	REFLOW
C11	RF grade 0402 ceramic	1pf	REFLOW
R5	generic 0402 thick film	10k	REFLOW
R6	generic 0402 thick film	12k	REFLOW
R7	generic 0402 thick film	2k	REFLOW
C30	generic 0402 ceramic	.1uf	IRON
C31	generic 0402 ceramic	.1uf	IRON
c17	RF grade 0402 ceramic	56pf	IRON
ANT	Custom	Antenna	IRON

<b>Table 4.2-4</b>	Components	for	assembly	in	step	4
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After assembly the communication system functionality should be verified. Please refer to "Communication initial test" in testing procedures.

#### 4.2.4 Attitude Determination and Control

Continue assembly on a PCB populated with the Power, C&DH and Communication systems, which have been verified for Power, C&DH and communication "Initial test" functionality. Assemble the following components in the order listed.

Schematic name	Manufacturer PN	Description	Solder method
MAG	MS2100	Magnetometer	REFLOW
R+,R-	generic 0402 thick film	43 ohm	IRON
Zsense	SEN-Z	z axis sense inductor	IRON
H1,H2,H3	A3903	H bridge	REFLOW
LA,LB		Magnetic torque rods	IRON
LZ		Magnetic torque coil	IRON

Table 4.2-5 Components for assembly in step 5

After assembly ADAC system functionality should be verified. Please refer to "Attitude Determination and control initial test" in testing procedures.

#### 4.2.5 Payload

Continue assembly on a PCB populated with the Power, C&DH, Communication and ADAC systems, which have been verified for Power, C&DH, Communication and ADAC "Initial test" functionality. Assemble the following components in the order listed.

Table 4.2-6 Components for assembly in step 6

Schematic name	Manufacturer PN	Description	Solder method
BS1	ADG3248	Bus switch	REFLOW
CAM	COMmedia C328	VGA camera	IRON

After assembly Payload system functionality should be verified. Please refer to "Payload test" in testing procedures.

# 4.3 Testing procedures

#### 4.3.1 Power subsystem initial test

After assembling the basic power system the regulated voltage must be tested over the input voltage range to ensure the safety of all components dependant on this system. The power system is capable of damaging the rest of the satellite if the output voltage is too high, or fluctuates rapidly.

This test shall be performed with a bench power supply of adjustable voltage as a replacement for the battery. Initially the bench supply shall limit the current into the regulator to less than 100mA to prevent damage in the event of total device failure. The current limit shall be increased thereafter to suit the needs of the test.

Parameter	Value	Conditions
Voltage	3.0±.010 Volts	3.2V @ input, no load @ output
	3.0±.010 Volts	4.2V @ input, no load @ output
	3.0±.010 Volts	3.2V @ input, 100mA load @ output
	3.0±.010 Volts	4.2V @ input, 100mA load @ output
	3.0±.100 Volts	3.2V @ input, 750mA load @ output
	3.0±.100 Volts	4.2V @ input, 750mA load @ output
	0 Volts	DEP_SW held open

Table 4.3-1 Power system test parameters

All test loads shall be removed from the DUT after test is completed

#### 4.3.2 Command and Data handling subsystem initial test

The processor which forms the core of the C&DH, as well as the basis for the entire satellite must be operational at this stage. This test shall be performed with a bench power supply of fixed voltage as a replacement for the battery. The power supply fixed voltage shall be 3.3 volts  $\pm 0.01$  volts, this voltage shall be verified by a meter external to the supply. The current limit for this test shall be 100mA at the supply. Perform the following steps to prepare the DUT for this trial:

- Using IAR embedded workbench attempt to program the C&DH with the "C&DH initial test" code base. The C&DH should program flawlessly and the test code should execute after the programming has completed.
- ii. The following parameters should be observed to verify code execution

Parameter	Value	Conditions
SPI bus	Activity	Periodic
P0.2	.5 duty PWM	All
P0.3	.5 duty PWM	All
P0.4	.5 duty PWM	All
P1.1	.5 duty PWM	All
P1.0	.5 duty PWM	All

Table 4.3-2 Command and Data handling subsystem test parameters

#### 4.3.3 Communication subsystem initial test

The communication system will be required for later, more complex debugging procedures. The communication system is capable of generating hazardous microwave radiation at the antenna. Health Canada safety Code 6 defines the maximum exposure limits for RF frequencies in the 3kHz to 300GHz range; the maximum field power density for 2.4GHz band is 10  $W/m^2$ . The emitted power form the femtosatellite communication system is a maximum of 500mW, in a cone of 120 degrees, hence the minimum radius from the antenna face of the satellite is

$$r = \frac{\sqrt{\frac{\rho_e}{\pi\rho_l}}}{\tan(\frac{\theta}{2})} = 7.2 \, cm \tag{4.1}$$

Additionally, the Specific absorption rate (SAR) for the human body must be below 0.08 W/kg, and for the human eye especially must be below 0.2 W/kg (Health Canada, 1999), therefore it is strongly recommended that no persons or animals be within one meter of the antenna within its cone of emission. Further take note that metal and concrete objects illuminated by the antenna will reflect RF energy, potentially back at the operator. A licensed

amateur radio operator shall be present at all times during testing to act as the control operator of the station

This test will be performed with a bench power supply of fixed voltage of 3.7 V as a replacement for the battery. The current limit for this test shall be set to 750 mA at the supply. Perform the following steps to prepare the DUT for this trial:

- i. Using IAR embedded workbench load the C&DH with the "communication initial test" codebase. The C&DH should program flawlessly and the test code should execute after programming has completed.
- ii. Using IAR embedded workbench load the SmartRF04 USB key evaluation module with the "Communication-USB" codebase.
- A terminal program shall be used on the host computer, configured to use the SmartRF04 USB key comport with settings 9600 8-N-1
- iv. To prevent damage to the SmartRF04 USB key have 5 meters of space between the femtosatellite and the USB key.
- v. The following parameters should be observed to verify code execution

Parameter	Value	Conditions	
Loopback	functional		
Current	<100 mA	during reception	
	>400 mA	during transmission	
Vramp	1.5 V	during transmission	
RSSI	>-30dBm	at USB key, during transmission, 5m range	

Table 4.3-3 Communication system test parameters

#### 4.3.4 Attitude Determination and Control initial test

The ADAC subsystem is checked in this section for proper operation. "F", "R", "S" and "H" commands are issued through a terminal program on the host computer to evaluate various test parameters. The satellite test code will interpret these commands autonomously.

This test will be performed with a bench power supply of fixed voltage of 3.7V as a replacement for the battery. The current limit for this test shall be set to 750 mA at the supply. Perform the following steps to prepare the DUT for this test:

- i. Using IAR embedded workbench load the C&DH with the "Attitude initial test" codebase. The C&DH should program flawlessly and the test code should execute after programming has completed.
- ii. Using IAR embedded workbench load the SmartRF04 USB key evaluation module with the "Communication-USB" codebase.
- A terminal program shall be used on the host computer, configured to use the SmartRF04 USB key comport with settings 9600 8-N-1
- To prevent damage to the SmartRF04 USB key have 5 meters of space between the femtosatellite and the USB key.
- v. The following parameters should be observed to verify code execution

Parameter	Value	Conditions
V_LA	.5 duty PWM	initial start, "H" command issued
	+3.0 V	"F" command issued
	-3.0 V	"R" command issued
	0 V	"S" command issued
V_LB	.5 duty PWM	initial start, "H" command issued
	+3.0 V	"F" command issued
	-3.0 V	"R" command issued
	0 V	"S" command issued
V_LZ	.5 duty PWM	initial start, "H" command issued
	+3.0 V	"F" command issued
	-3.0 V	"R" command issued
	0 V	"S" command issued
Magx	Geomagnetic	"S" command issued
Magy	Geomagnetic	"S" command issued
Magz	Geomagnetic	"S" command issued

Table 4.3-4 Attitude determination and control test parameters

## 4.3.5 Payload system

The payload system uses the camera module, flash ram and CDH to shuffle data from the camera buffer to the host computer. A terminal program is used to issue "T" and "I" commands to the satellite, and the satellite will interpret these commands autonomously. This test will be performed with a bench power supply of fixed voltage of 3.7V as a replacement for the battery. The current limit for this test shall be set to 750 mA at the supply. Perform the following steps to prepare the DUT for this trial:

- Using IAR embedded workbench load the C&DH with the "payload system test" codebase. The C&DH should program flawlessly and the test code should execute after programming has completed.
- ii. Using IAR embedded workbench load the SmartRF04 USB key evaluation module with the "Communication-USB" codebase.
- A terminal program shall be used on the host computer, configured to use the SmartRF04 USB key comport with settings 9600 8-N-1 to issue the commands to the DUT.
- To prevent damage to the SmartRF04 USB key have 5 meters of space between the femtosatellite and the USB key.
- v. The following parameters should be observed to verify code execution

Parameter	Value	Conditions
SPI bus	Activity	"I" command issued
Radio	Activity	"T" command issued

#### Table 4.3-5 Payload system test parameters

Upon issuing the "T" command the C&DH will pause for 2 seconds to allow the user to set up a file capture in the users terminal software. Promptly thereafter the image taken and stored with the "I" command will be transmitted via the radio interface. The captured file can be viewed as a JPEG format file to verify payload system functionality.

## 4.3.6 Simulated environment

The simulated environment testing is designed to test the femtosatellites reaction to a simulated space environment. In this test the femtosatellite will received simulated sensor readings generated by the host computer. In return, the femtosatellite will telemeter its attitude determination and control input information back to the host computer for processing. The host computer will apply the desired control efforts to the simulated model and evaluate the performance of the femtosatellites control system. Perform the following steps to prepare the DUT for this trial:

- Using IAR embedded workbench load the C&DH with the "integrated system test" codebase. The C&DH should program flawlessly and the test code should execute after programming has completed.
- Using IAR embedded workbench load the SmartRF04 USB key evaluation module with the "Communication-USB" codebase.
- To prevent damage to the SmartRF04 USB key have 5 meters of space between the femtosatellite and the USB key.

iv. Start Matlab/Simulink and load the "Hardware-in-the-loop" model With the execution of the simulink model, the femtosatellite will receive simulated sensor readings based on the propagated model. All control efforts the femto exerts will be dually applied to the magnetic torquers and the model. The estimated attitude will also be reported to the simulink model for comparison against the propagated attitude.

#### 4.3.7 Integrated satellite system

The integrated satellite system must finally be tested against the harsh launch and space environments. In this test the femtosatellite will be subjected to launch vibrations, and the vacuum and thermal conditions of low earth orbit.

#### Launch vibration testing:

The reference launch environment used for this test is the one found in the Dnepr launch vehicle (Kosmotras, 2001). The femtosatellite shall be subjected to 6.5g RMS vibration (20Hz to 2kHz) on all axes for a duration of 35 seconds to simulate launch vehicle liftoff. The femtosatellite shall then be subjected to 3.6g RMS vibration (20Hz to 2kHz) for a

duration of 831 seconds to simulate launch vehicle flight. This test will be conducted with the deploy switch in the off (not deployed) state.

At the conclusion of the test the femtosatellite shall be fully functional with no apparent mechanical damage.

## Space environment testing:

The femtosatellite shall be subjected to vacuum testing while undergoing thermal cycling similar to the thermal extremes it is expected to experience in orbit. This test will be conducted with the satellite fully operational and telemetering health data at full RF power. At the conclusion of the test the femtosatellite shall be fully functional with no evidence of performance degradation.

# 4.4 Results

#### 4.4.1 **Power subsystem initial test**

Voltage was measured at the cc2510 reset pullup resistor *Rpu* using a LeCroy WaveSurfer 24xs digital oscilloscope.

Parameter	Value	Conditions	Measurement	Result
Voltage	3.0±.010 V	3.2 V @ input, no load @ output	3.0±0.006	PASS
	3.0±.010 V	4.2 V @ input, no load @ output	3.0±0.006	PASS
	3.0±.010 V	3.2 V @ input, 100mA load @ output	3.0±0.006	PASS
	3.0±.010 V	4.2 V @ input, 100mA load @ output	3.0±0.006	PASS
	3.0±.100 V	3.2 V @ input, 750mA load @ output	3.0±0.006	PASS
	3.0±.100 V	4.2 V @ input, 750mA load @ output	3.0±0.006	PASS
	0 V	DEP_SW held open	0.006	PASS

Table 4.4-1 Power subsystem test results

The measured output ripple voltage includes the noise in the oscilloscopes measurements. It should be noted that the oscilloscope shows 6mv of noise when and input is disconnected

from all sources and shorted to ground at the connector, hence the ripple performance of the converter is better than the scopes ability to measure it.

## Battery ripple rejection

The battery and bus voltage were monitored during a telemetry broadcast. This represents a load step to the power system of almost 500mA from an idle condition of 80mA. The Figure 4.4-1 through Figure 4.4-3 illustrate the robustness of the power system to rapid load changes and high noise on the battery side of the converter.



Figure 4.4-1 Battery voltage ripple from telemetry broadcast



Figure 4.4-2 Bus voltage ripple during telemetry broadcast





# 4.4.2 Communication subsystem initial test

The communication system was tested with an RF datarate of 10kbps. The results demonstrate the functionality of the RF implementation.

Parameter	Value	Conditions	Measurement	Result
Loopback	Functional	Powered	Functional	PASS
Current	<100 mA	during reception	80 mA	PASS
	>400 mA	during transmission	420 mA	PASS
Vramp	1.5±.1 V	during transmission	1.58 V	PASS
RSSI	>-30 dBm	at USB key, during transmission, 5m range	-29 dBm	PASS

Table 4.4-2 Communication subsystem test results

## 4.4.3 Attitude determination and control subsystem initial test

The attitude determination and control system was tested. All measurements were within expected tolerances.

Parameter	Value	Conditions	Measurement	Result
V_LA	.5 duty PWM	initial start, "H" command issued	0.5	PASS
	+3.0 V	"F" command issued	2.95 V	PASS
	-3.0 V	"R" command issued	-2.97 V	PASS
	0 V	"S" command issued	0 V	PASS
V_LB	.5 duty PWM	initial start, "H" command issued	0.5	PASS
	+3.0 V	"F" command issued	2.92 V	PASS
	-3.0 V	"R" command issued	-3.0 V	PASS
	0 V	"S" command issued	0 V	PASS
V_LZ	.5 duty PWM	initial start, "H" command issued	0.5	PASS
	+3.0 V	"F" command issued	2.99 V	PASS
	-3.0 V	"R" command issued	-2.95 V	PASS
	0 V	"S" command issued	0 V	PASS
Magx	Geomagnetic	"S" command issued	±54 μΤ	PASS
Magy	Geomagnetic	"S" command issued	±54 μΤ	PASS
Magz	Geomagnetic	"S" command issued	±54 μΤ	PASS

#### Table 4.4-3 ADCS test results

# 4.4.4 Payload subsystem initial test

The payload system was tested on the prototype. The image was captured and transmitted in approximately 20 seconds at an RF data rate of 10kbps. The captured image is presented below.



Figure 4.4-4 Captured image from femtosatellite prototype payload system.

## 4.4.5 Simulated environment test

Hardware in the loop testing was carried out on the prototype. A summary of the parameters assumed during the simulation can be found in Table 3.5-1 in section 3.5.5. In addition to these parameters, the following were also implemented:

Parameter	Value
t <sub>s</sub> Sampling time	1 <i>s</i>
$t_d$ Sensor $\rightarrow$ controller time lag	1 <i>s</i>
Magnetic torquer saturation	$\pm .01 \ amp \cdot turn \cdot m^2$
Magnetic torquer quantization step size	$7.8125 \cdot 10^{-5} amp \cdot turn \cdot m^2$
Hardware floating point number format	Single precision 32 bit

Table 4.4-4 Simulated environment additional parameters

Figure 4.4-5 to Figure 4.4-7 show the response of the simulated satellite in the space environment to the actual controller onboard the femtosatellite. These plots differ greatly from the ideal simulation case due to the impact of quantization on the magnetic actuators. Numerical noise introduced by the single precision floating point was mitigated by measuring magnetic fields in micro Tesla, and calculating control torques in micro Newton meters, which pushes the expected values towards practical values for this number format. Figure 4.4-7 shows a detailed view of the quantization noise which causes the difference in the plots. Overall this test indicates that the system would perform better with a smaller quantization step size, which can be realized with either smaller magnetic torque actuators (less windings or less current) or more bits in the output stage. As the simulations to date have not saturated the best option would be to reduce the magnetic torque rod moment to conserve mass or power.



Figure 4.4-5 Hardware in the loop simulated Euler angles for one orbit



Figure 4.4-6 Hardware in the loop applied dipole moments for one orbit


Figure 4.4-7 Detailed view of dipole moments during first 100 seconds of orbit

Additionally one of the output pins of the microprocessor was assigned to a value of 1 during the period of calculation. The execution of the control law and magnetic mapping law takes on average  $520 \ \mu s$  as shown in Figure 4.4-8.



Figure 4.4-8 Pulse indicating duration of control law calculation

#### 4.4.6 Structure finite element analysis

Finite element analysis was performed on the proposed structure to test deflection and natural frequencies under launch conditions. The Dnepr users guide lists the maximum longitudinal acceleration as 7.5 G, and indicates that harmonic oscillations occur at frequencies of up to 20 Hz. For smooth integration with the launch vehicle the natural frequencies of the payload should be greater than 20 Hz in the longitudinal axis and 10 Hz laterally. It is expected that these requirements are typical of most available launch systems. (Kosmotras, 2001)

Solidworks 2009 was used to perform the finite element analysis. A three dimensional polygon mesh was employed, with 4 Jacobian points per element. The results represent a first order analysis and indicate that mechanical testing can proceed with a likelihood of success.

The structure was placed under a load of 7.5 G and the deflection was evaluated as shown in Figure 4.4-9. As expected, the sun side solar array experiences the greatest displacement, with a peak deflection of  $23 \,\mu m$ . Safety factor was also evaluated under a static load of 7.5 G, and the minimum safety factor was found to be 26.9. Additionally the natural frequencies of the structure were evaluated. The natural frequencies were found to be all in excess of 100 Hz, indicating that the structure is very rigid. The results are tabulated in Table 4.4-5, and Figure 4.4-11 illustrates the numbered modes.



Figure 4.4-9 Deflection as a result of 7.5g static load



Figure 4.4-10 Safety factor distribution for 7.5g static load

Mode shape	Natural Frequency
1	115.68 Hz
2	165.1 Hz
3	291.58 Hz
4	335.31 Hz

Table 4.4-5 Natural frequencies for various resonant modes



Figure 4.4-11 Resonant modes of femtosatellite structure

# 4.4.7 Thermal simulations

Matlab/Simulink was used to perform thermal simulations of the femtosatellite in orbit. A summary of the parameters assumed during the simulation can be found in Table 3.5-1 in section 3.5.5. As shown in Figure 4.4-12 the sunside array undergoes large temperature swings on orbit, from 72.6 degrees Celsius to -39.2 degrees Celsius. The printed circuit board and battery are buffered from the sun by the array and scaffolding and thus remain bounded by 65 degrees and -37 degrees. All components on the satellite have been chosen for their -40 to 85 degree survivability. The temperature rates illustrated in Figure 4.4-13 are bounded by  $\pm 0.1$  deg/sec. Heating and cooling rates on this order will create negligible thermal shock on the system.



Figure 4.4-12 Temperature of the three major nodes for two orbits



Figure 4.4-13 Temperature rates of the three major nodes for two orbits

# Chapter 5 Conclusions

# 5.1 Conclusions

Femtosatellites are poised to take advantage of Moore's law by offering the smallest path to space for advancing technologies. The low launch costs and ability to launch redundant systems in parallel allow the use of riskier COTS technology in space. The usage of COTS technology drastically cuts development budget and lead time, which enables more hardware to be flown. This is a virtuous development cycle, which allows for faster development of new space technologies. A femtosatellite design has been shown to fulfill the basic requirements of a satellite system. The enabling features of the femtosatellite system are enumerated below.

# 5.1.1 Communications

The femtosatellite is capable of matching existing cubesat communication abilities in terms of datarate and ground contact capability with a fraction of the mass and space requirements. The capacity for high speed data communications and reconfigurable broadcast frequency sets this design apart from conventional cubesats in that large payload data objects and various regulatory hurdles can be accommodated quickly at the software level on orbit.

# 5.1.2 Attitude determination and control

The femtosatellite is capable of nominal pointing missions with simulated pointing accuracy of approximately 5 degrees. This unlocks the capacity for a variety of low resolution earth

observation missions where pointing must be known and stabilized. Further capacity exists as an inspector satellite, where the same imaging hardware can be used for high resolution inspection of a larger satellite system in low earth orbit.

### 5.1.3 Structure

Survivability of the femtosatellite has been demonstrated through finite element analysis. The femtosatellite is constructed from rigid materials and is extremely lightweight, contributing greatly to the stiffness of the satellite system. Due to the lightweight nature of the satellite components and the small deflections expected, the use of solder and epoxy for mechanical fastening is justified.

# 5.2 Future work

#### 5.2.1 Magnetic control

Better attitude performance may be achieved though investigation of various magnetic control schema. As this femtosatellite offers a full complement of magnetic torquers, it stands to benefit directly from more advanced algorithms. The low launch mass of this system makes it ideal for on orbit testing and validation of control

### 5.2.2 Simulated environment test

Hardware in the loop testing is very important for the verification of the performance of the femtosatellite, particularly the ADCS algorithms. The limitations imposed by the finite numerical performance of the processor and discrete sampling time should be explored to maximize the systems potential.

# 5.2.3 Orbit reconfiguration and formation flying using aerodynamic drag

Given that the ballistic coefficient of the femtosatellite varies by a factor of 10 with attitude, this opens the possibility of active orbit reconfiguration, or differential drag formation flying. Large numbers of femtosatellites could be deployed in orbit with minimal cost. Each node can communicate with each other node and with the ground to fulfill autonomous control and payload requirements.

# 5.2.4 Launch

Finally the fully integrated femtosatellite should be fitted to a host vehicle for deployment in low earth orbit as a validation of the work.

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